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## Prediction of Payload Internal Pressure

CHRISTOPHER P. KREBS

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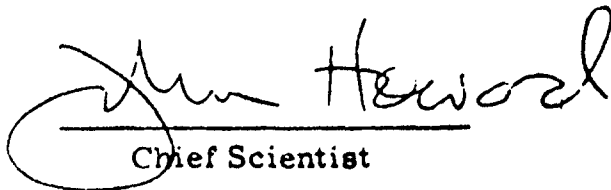


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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) → An analysis of the internal pressure history of sounding rocket payloads as they ascend through the atmosphere was conducted. The analysis was concerned mainly with compressible flow and included the affects of choking. Computer programs were developed that successfully predict the internal pressure from trajectory data. The programs were based on both the theoretical analysis and mathematical models of the flow rates of various venting components used in relieving the payload internal pressure. The mathematical models were developed from empirical data gathered during		

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testing. The payload model can be set up with any combination of relief<sup>f</sup> valves and air filters, and has provisions for including leaks due to doors and seals. Sample program results for several payloads are included along with the program listings.

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## Prediction of Payload Internal Pressure

### 1. INTRODUCTION

Difficulties on several rocket flights in the recent past have been linked to the build-up of the internal pressure of the payload. This increase produced an environment that was adverse to the operation of components of the payload, resulting in their malfunction or failure. To determine the affects of these unfavorable conditions, it was necessary to calculate the internal pressure as a function of time. The analysis contained herein was performed to accomplish this task. It consisted of the mathematical development of the differential equations that represent the modelled pressure functions and the subsequent utilization of a digital computer to determine their solution. The computer programs and their results have been verified by comparison to empirical data. These supplementary programs can be used in after-the-fact calculations of the pressure the payload experienced for a particular rocket flight. A more useful approach would be to use them analytically to predict the internal pressure of a payload under design. In this manner, possible pressure problems can be found and corrected in advance of the actual flight.

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(Received for publication 3 September 1980)

## 2. SINGLE VOLUME MATHEMATICAL ANALYSIS

The problems from pressure build-up arise from the fact that the internal gas cannot vent fast enough to lower the payload pressure. A pressure differential is formed which results in loads to sensitive items such as doors, compartments and components, causing damage, malfunction, or inoperation of these devices.

On the launch pad, the payload is usually pressurized to insure that the "clean" area is at a slightly higher pressure than the surrounding environment. In this manner, dust particles can be kept from contaminating the important payload areas. As the rocket ascends through the atmosphere the external pressure drops faster than the payload pressure can follow, creating a differential between the internal and external pressures.

The payload is modelled as a simple box of volume equal to the volume of gas to be vented. To this box is attached the venting apparatus of the payload, as shown in Figure 1. The configuration consists of any combination of valves, filters and orifices used in relieving the internal pressure of the payload. The only way for the internal pressure of the payload to be released is through the venting apparatus and any leaks. With the proper design configuration, the internal pressure can be made to approximately track the external pressure.

The valves are closed until the pressure differential across them is equal to or greater than their cracking pressure. The filters are open and operating at all times. Provision is included for any leaks due to doors or seals, which are modelled as orifices with an effective exit area. More will be presented on the operating characteristics of these devices later in this report.

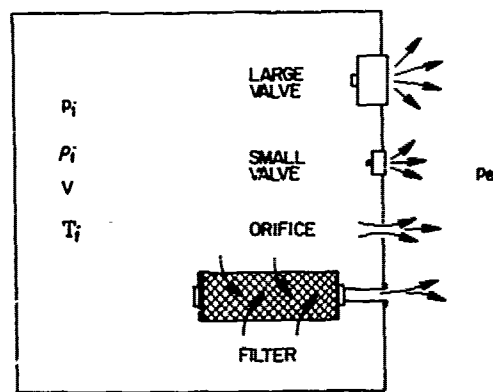


Figure 1. Payload Model for Venting Analysis



The mathematical analysis is begun by writing the perfect gas law for the fluid in the box:

$$p_i = \rho_i R T_i = m_i R T_i / V. \quad (1)$$

Differentiating with respect to time, we obtain

$$\frac{dp_i}{dt} = \frac{d}{dt} \left[ \frac{m_i R T_i}{V} \right] = \frac{R}{V} \left[ T_i \frac{dm_i}{dt} + m_i \frac{dT_i}{dt} \right] \quad (2)$$

For simplicity, the internal temperature will be assumed to be constant throughout the flight. The average ascent through the atmosphere lasts 80 sec; this does not allow enough heat to be transferred to or from the gas to significantly change its temperature. Then Eq. (2) becomes

$$\frac{dp_i}{dt} = \frac{R T_i}{V} \frac{dm_i}{dt} = \frac{R T_i}{V} \dot{m}_i \quad (3)$$

where  $dp_i/dt$  is negative for  $p_i > p_e$ . To calculate the internal pressure from Eq. (3), we need to determine the rate of change of the mass in the box. The fluid mass is decreased by the flow through the venting apparatus, which is governed by the flow characteristics of the valves, filters and orifices. These characteristics have been measured experimentally from actual hardware and are presented in detail in Appendix A.

The mass flow rate is a function of the density of the gas and the pressure differential across the device, which is defined as:

$$\Delta p = p_{int} - p_{ext} \quad (4)$$

The external pressure is taken as the atmospheric pressure (at altitude) that the payload experiences, which can be determined from the rocket's trajectory. Aerodynamic affects producing a pressure coefficient and a subsequent change in the "external" pressure are ignored for the following reasons:

- (1) In all cases analyzed so far, the valves and filters have been mounted on the cylindrical sections of the payloads, for which  $c_p$  is negligible or zero;
- (2) The effects of angle of attack and boundary layers are considered to be negligible.

The total mass flow rate is the sum of the contributions of the individual venting components:

$$\dot{m}_T = \dot{m}_v (\# \text{ of valves}) + \dot{m}_f (\# \text{ of filters}) + \dot{m}_o. \quad (5)$$

From the considerations of continuity, we find that the rate of change of the internal gas mass is equal to the rate at which the gas leaves the volume:

$$\dot{m}_i = -\dot{m}_T. \quad (6)$$

Using this substitution, the differential equation which models the payload internal pressure becomes

$$\frac{dp_i}{dt} = - \frac{RT_i}{V} \dot{m}_T. \quad (7)$$

With the external pressure as a function of time and the equation for the mass flow rate, the above differential equation can be integrated to give the internal pressure as a function of time.

### 3. COMPUTER PROGRAM PRESSLFOR

Equation (7) can be integrated numerically to obtain the internal pressure at any time through the use of a digital computer. The general ordinary differential equation of the form  $dy/dx = f(x, y)$  with initial condition  $y_0 = f(x_0)$ , is solved using a fourth-order Runge-Kutta integration process. This is a single-step method in which the value of  $y$  at  $x = x_n$  is used to compute  $y_{n+1} = y(x_{n+1})$ . The relevant formulas for integration are:

$$y_{n+1} = y_n + \frac{1}{6} (T_1 + 2T_2 + 2T_3 + T_4) \quad (8)$$

where

$$\begin{aligned} T_1 &= hf(x_n, y_n) \\ T_2 &= hf(x_n + h/2, y_n + T_1/2) \\ T_3 &= hf(x_n + h/2, y_n + T_2/2) \\ T_4 &= hf(x_n + h, y_n + T_3) \\ h &= \text{step size} . \end{aligned} \quad (9)$$

A step size of 0.01 sec was selected for this program. The schematic of Figure 2 gives a visual representation of the integration process. The y values defined at intermediate steps are used to calculate the future y values, without using any previous results. The method is a quick and efficient means of integrating a differential equation.

This integration technique and the differential equation have been programmed on the PDP-11/34 computer using the FORTRAN IV language. A listing and flow chart of program PRESS4.FOR are presented in Appendix B.

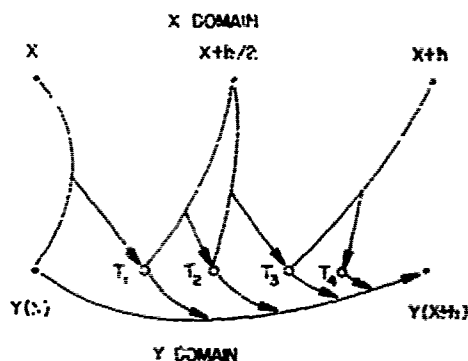


Figure 2. Integration Schematic.

#### 4. MULTIPLE VOLUMES MATHEMATICAL ANALYSIS

A payload can be constructed such that interconnected compartments are involved in the venting process. The model of this case consists of boxes connected by various venting components, as shown in Figure 3 for two volumes. The main volume, box No. 1, is set up in a manner similar to the single volume model: with valves, filters, and orifices exposed to the external environment. The major difference is that it now has fluid input from the secondary volume. The secondary volume, box No. 2, is set up for venting gas to both the main volume (through valves) and the external environment (through filters and orifices).

For volume No. 1, the mass flow rate is

$$\dot{m}_1 = -(\dot{m}_{T1} - \dot{m}_{T2}) \quad (10)$$

where  $\dot{m}_{T1}$  is the flow rate output of the main venting apparatus and  $\dot{m}_{T2}$  is the rate input from the second volume. For volume No. 2, the mass flow rate is

$$\dot{m}_1 = -\dot{m}_{T3}$$

(11)

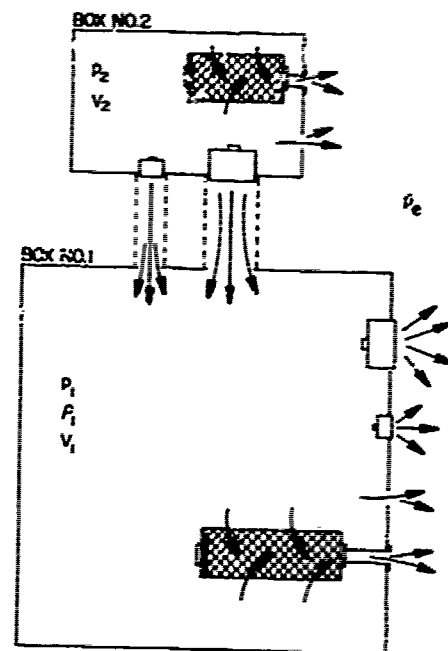


Figure 3. Payload Model  
for Multiple Volumes  
Venting Analysis

Proceeding in a manner analogous to the single volume analysis, we obtain two differential equations: one for each volume:

$$\frac{dp}{dt} 1 = - \frac{RT_1}{V_1} (\dot{m}_{T1} - \dot{m}_{T2}) \quad (12)$$

$$\frac{dp}{dt} 2 = - \frac{RT_2}{V_2} (\dot{m}_{T3}) \quad (13)$$

where

$$\begin{aligned} \dot{m}_{T1} &= \dot{m}_{v1} + \dot{m}_{f1} + \dot{m}_{o1} \\ \dot{m}_{T2} &= \dot{m}_{v2} \\ \dot{m}_{T3} &= \dot{m}_{T2} + \dot{m}_{f2} + \dot{m}_{o2} \end{aligned} \quad (14)$$

This analysis can be extended to include an infinite number of volumes, obtaining  $n$  differential equations for  $n$  volumes interconnected together and venting to the atmosphere.

#### 5. COMPUTER PROGRAM PRESSM.FOR

A two-volume venting calculation has also been programmed on the PDP-11/34 computer. The numerical integration process is similar to that used for the single-volume problem; here it is set up for a system of ordinary differential equations. The method is contained in the FORTRAN IV subroutine RKGS.FOR in the IBM Scientific Subroutines Manual (Reference 4). A listing and flowchart of program PRESSM.FOR are presented in Appendix C.

#### 6. SAMPLE PROGRAM RESULTS

The two computer programs referenced in this report have been used to analyze payload designs. Presented here are the results for the SPICE, IRBS, and ZIP payloads. Also presented are the results of the test case used to verify program operation and validity.

##### 6.1 SPICE Payload

The SPICE payload was flown on 27 Jan 1979 and experienced failure of the door unlatching mechanism. The cause of this failure was determined to be a buildup of the internal pressure which resulted in increased loading on the door. The SPICE payload was analyzed using an earlier version of the single volume computer program. Figure 4 is a plot of the computer results.

SPICE payload configuration:

Volume: 19.55 cu ft,

Venting apparatus: 2 P7-637 0.50 psi relief valves.

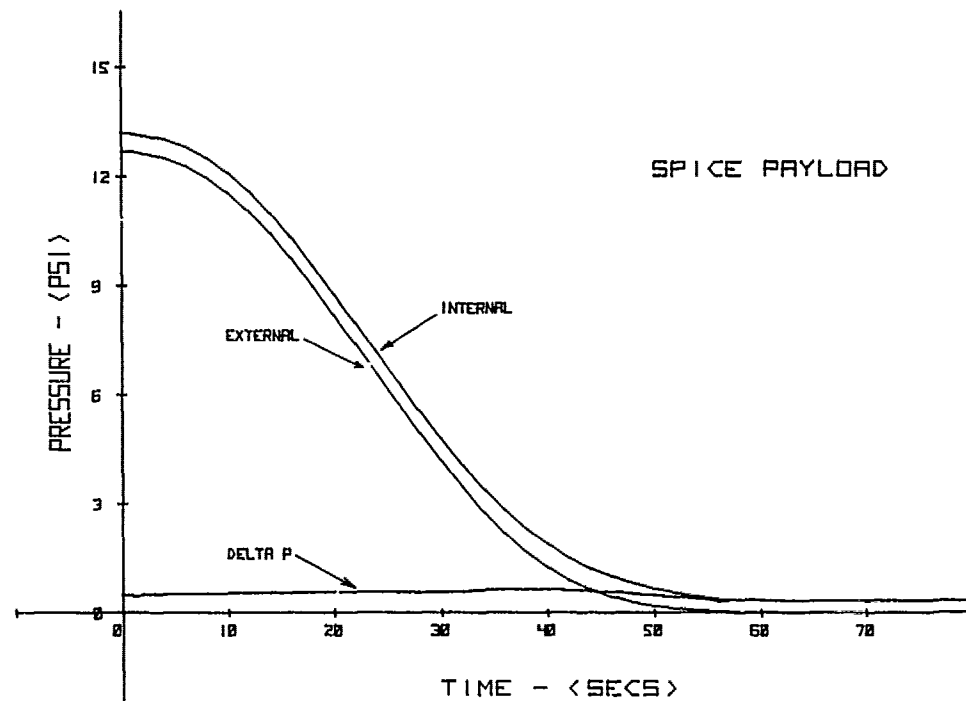


Figure 4. Program Results for SPICE Payload

## 6.2 IRBS Payload

The IRBS payload was analyzed during the testing phase. It consists of a small chamber venting into the larger main volume of the payload. The intent here was to determine the maximum internal pressure that the payload would experience in order to generate proper testing levels. Figure 5 is a plot of the program results for Volume No. 1; Figure 6 shows those for volume No. 2. Notice that the valves on the secondary volume do not operate at all; this is shown by the secondary volume internal pressure being lower than the main volume pressure in Figure 6. The leak takes care of any pressure build-up in volume No. 2.

IRBS configuration:

Volume No. 1: 46.80 cu ft,

Venting apparatus: 3 P7-637 0.50 psi relief valves venting to the atmosphere,

Volume No. 2: 0.18 cu ft,

Venting apparatus: 2 P-249 0.10 psi relief valves venting to the main volume; 1 leak (orifice) with effective area of 0.000042 sq ft venting to the atmosphere.

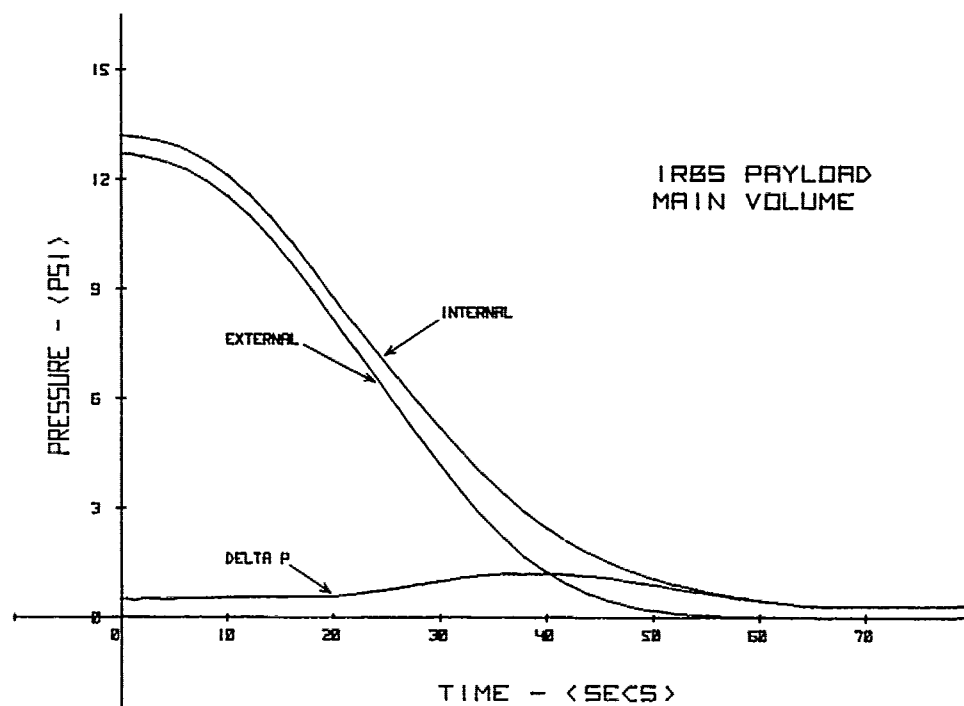


Figure 5. Program Results for IRBS Payload - Main Volume

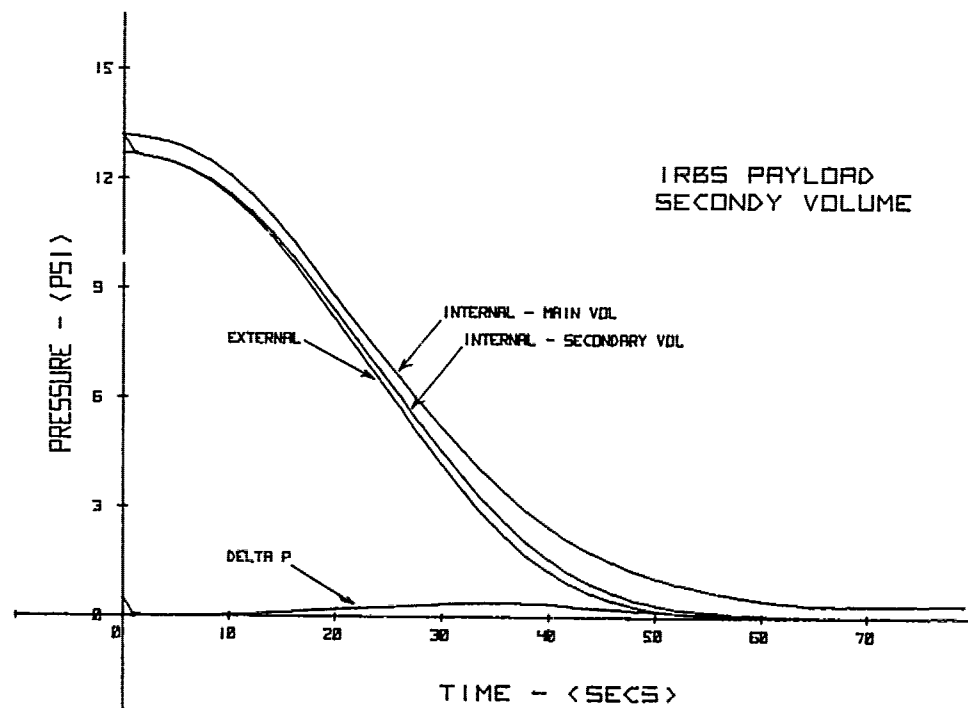


Figure 6. Program Results for IRBS Payload—Secondary Volume

### 6.3 ZIP Payload

The ZIP payload was analyzed during the design phase. It is a good example of how the programs can be used to pin-point problems in advance. The original analysis of ZIP showed a maximum delta p of over 1.69 psi; it also showed 0.187 psi at the critical time of door unlatching and opening (see Figure 7). The venting configuration was revised to include the larger relief valves. Subsequent reanalysis showed a much improved situation: the maximum delta p was decreased to just over 0.50 psi. Figure 8 presents the revised pressure prediction for the ZIP payload.



ZIP configuration:

Volume: 6.80 cu ft,  
Original venting: 6 P-249 0.10 psi relief valves,  
2 RA-2500 filters 0.11045 sq in. in area,  
Revised venting: 10 P-249 0.10 psi relief valves,  
4 P7-637 0.50 psi relief valves,  
2 RA-2500 filters 0.11045 sq in. in area.

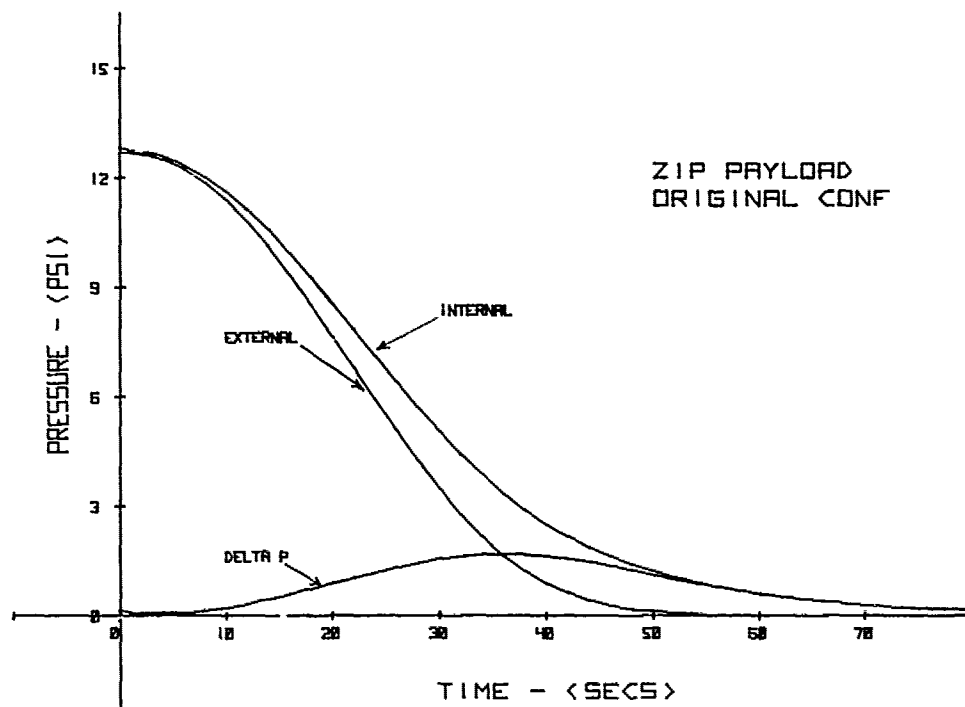


Figure 7. Program Results for ZIP Payload—Original Venting Configuration

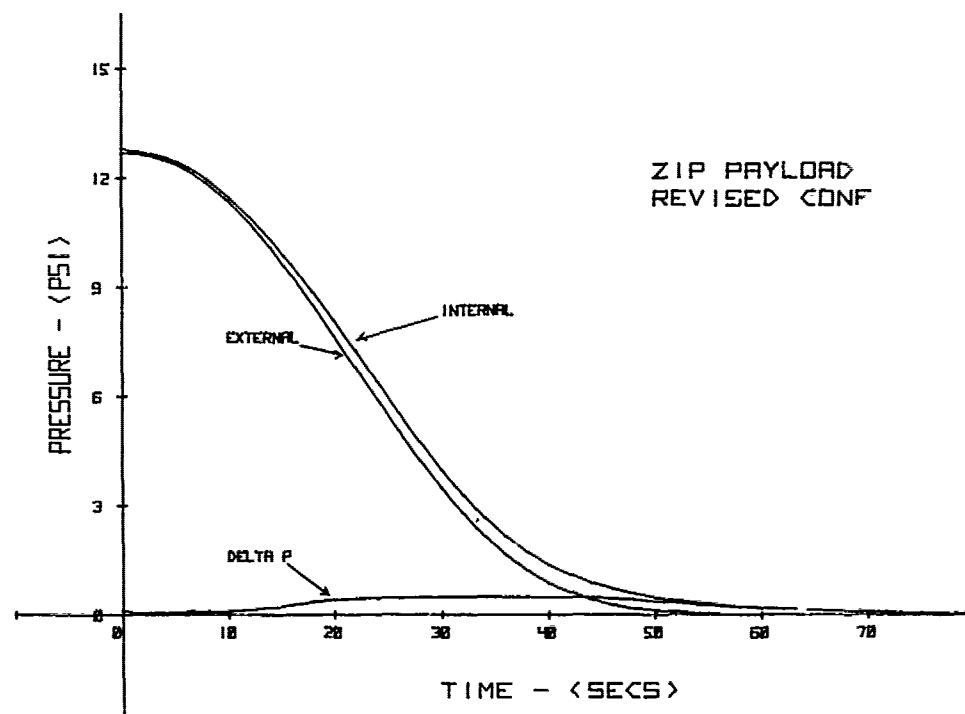


Figure 8. Program Results for ZIP Payload-Revised Venting Configuration

#### 6.4 Program Test Configuration

In order to validate the pressure programs, a test case was developed and evaluated during the ZIP payload analysis. A standard volume with only one relief valve was evacuated using a vacuum pump, such that the external and internal pressures were known to an accuracy of  $\pm 0.1$  psi. The test case results were then compared to those predicted by the computer program for the same external pressure variation. This comparison led to additional refinements in the programs, with subsequent improvement in their prediction capability. A comparison of the results follows in Figure 9. It is evident that the program has sufficient accuracy for design work while remaining slightly conservative.

##### Test configuration:

Volume: 1.00 cu ft,  
Venting apparatus: 1 P-249 0.10 psi relief valve.

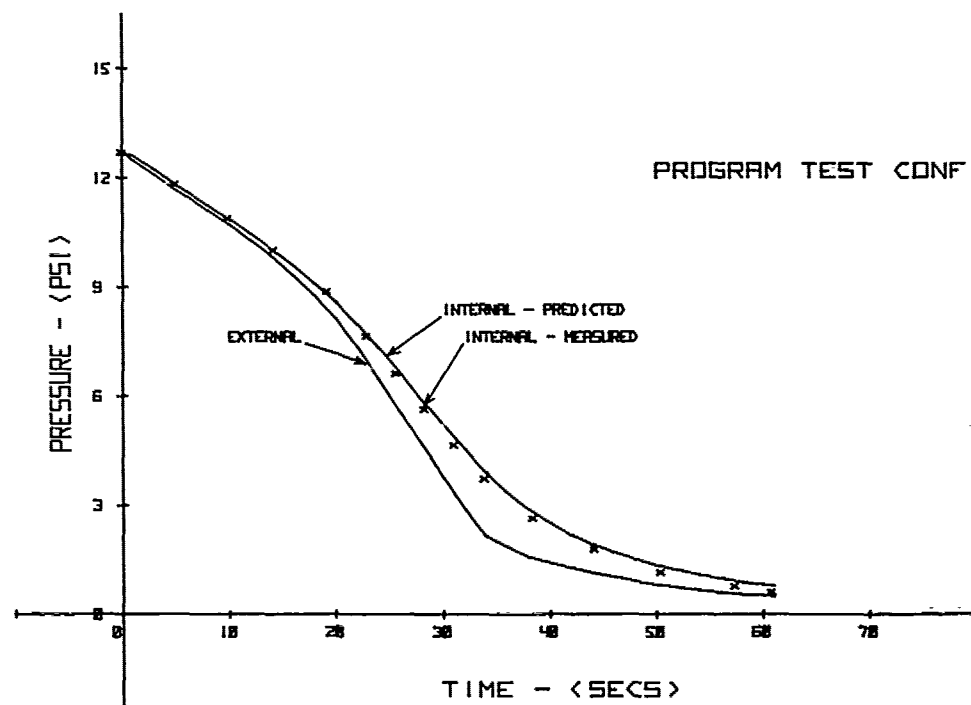


Figure 9. Program Results for Test Configuration

## References

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2. Blackburn, J. F., Reethof, G., and Shearer, J. L. (Editors) (1960) Fluid Power Control, MIT Press, Cambridge, MA, pp 54-55, 63-69, 214-220.
3. Shapiro, A. H. (1953) The Dynamics and Thermodynamics of Compressible Fluid Flow, Ronald Press, New York, pp 83-105.
4. IBM, System/360 Scientific Subroutine Package, Version III, Programmer's Manual, 5th Edition, 1970.
5. Lynch, W. P. (1979) SPICE I Failure Analysis, AFGL Technical Memorandum No. 19.

## Appendix A

### Operating Characteristics of Venting Components

The venting apparatus is analyzed as an opening of a certain area through which the fluid flows. The mass flow rate takes the form of

$$\dot{m} = \rho Q = \rho v A . \quad (A1)$$

The density of the fluid is a function of the pressure and the temperature and will be determined by inlet and outlet conditions. The volume flow rate depends upon the velocity of the fluid and the area of the opening. Both of these are functions of the fluid pressure. The velocity is related to the pressure ratio across the opening. In the case of the relief valves, the opening area is variable and is dependent upon the pressure differential. The cracking pressure on a valve is controlled by the properties of the helical spring which is part of the valve mechanism (see Figure A1). As the  $\Delta p$  is increased, the valve opens and the area of the opening is dependent upon how the spring is compressed. At some value of the pressure differential, the valve will "bottom out;" that is, the spring will reach maximum compression and the exit area will be at its greatest value.

We must also take into account compressibility effects and the phenomena of choking when analyzing the venting apparatus. The flow through an orifice (or any opening) can increase its velocity only until the Mach number reaches the value of 1. At this point the velocity in the throat (smallest area of the orifice) becomes sonic and the volume flow rate reaches its maximum value. Any attempt to further

increase the velocity through an increase in  $\Delta p$  will not be successful in changing the volume flow rate.

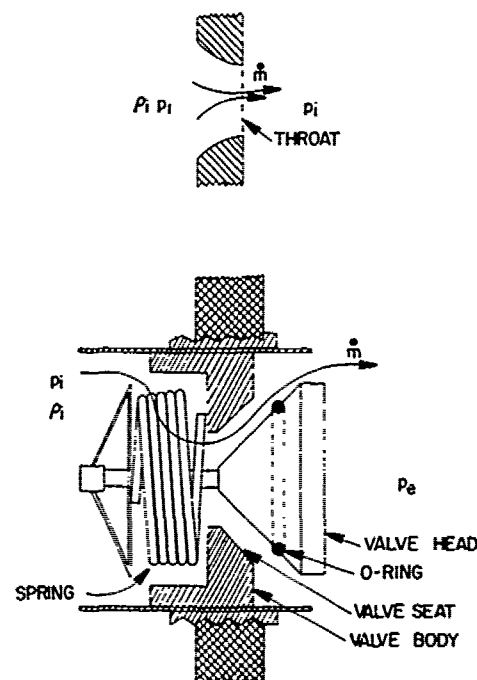


Figure A1. Throat Concept and Valve Mechanism

This is so because an increase in velocity would cause the Mach number at the throat to be greater than 1, which is an impossibility from fluid dynamics. When the velocity in the throat equals the speed of sound, the flow is said to be choked. The volume flow rate will remain constant, no matter how large the pressure differential becomes.

Choking is a function of the pressure ratio across the opening; here  $p_e/p_i$ . As the velocity increases and  $M$  approaches 1, the pressure ratio decreases. At a certain value of  $p_e/p_i$  the flow will reach  $M = 1$ ; this is called the critical pressure ratio and signals the onset of choking. A numerical value for the critical pressure ratio can be determined from fluid dynamics.

Writing Bernoulli's equation for compressible flow, we have

$$\frac{v_1^2}{2} + \int \frac{dp_1}{\rho_1} = \frac{v_c^2}{2} + \int \frac{dp_c}{\rho_c} = \text{constant} \quad (A2)$$

The velocity well away from the opening inside the volume is negligible; thus  $v_i = 0$  and

$$\int \frac{dp_i}{\rho_i} = \frac{v_e^2}{2} + \int \frac{dp_e}{\rho_e} . \quad (A3)$$

Rearranging the above equation, it becomes

$$\frac{v_e^2}{2} = \int \frac{dp_i}{\rho_i} - \int \frac{dp_e}{\rho_e} . \quad (A4)$$

From the relations of isentropic flow (frictionless, adiabatic flow of a perfect gas) we have the following:

$$p = C\rho^\gamma \quad \rho = (p/C)^{1/\gamma} \quad C^{1/\gamma} = \frac{p}{\rho} . \quad (A5)$$

Using this in Eq. (A4), it becomes

$$\frac{v_e^2}{2} = \int (C/p_i)^{1/\gamma} dp_i - \int (C/p_e)^{1/\gamma} dp_e \quad (A6)$$

$$\frac{v_e^2}{2} = C^{1/\gamma} \left( \int dp_i / p_i^{1/\gamma} - \int dp_e / p_e^{1/\gamma} \right) \quad (A7)$$

$$\frac{v_e^2}{2} = \frac{p_i^{1/\gamma}}{\rho_i} \left( \frac{p_i^{(1-1/\gamma)}}{(1-1/\gamma)} - \frac{p_e^{(1-1/\gamma)}}{(1-1/\gamma)} \right) \quad (A8)$$

$$\frac{v_e^2}{2} = \frac{p_i^{1/\gamma}}{\rho_i} (\gamma/\gamma-1) \left( p_i^{(\gamma-1)/\gamma} - p_e^{(\gamma-1)/\gamma} \right) \quad (A9)$$

$$\frac{v_e^2}{2} = \gamma/(\gamma-1) \frac{p_i}{\rho_i} \left( 1 - (p_e/p_i)^{(\gamma-1)/\gamma} \right) . \quad (A10)$$

Therefore, the exit velocity of the opening is given by

$$v_e = \sqrt{\frac{2\gamma}{\gamma-1} \frac{p_i}{\rho_i} \left( 1 - (p_e/p_i)^{(\gamma-1)/\gamma} \right)} . \quad (A11)$$

At Mach = 1,  $v_e$  will equal the speed of sound and  $p_e/p_i = (p_e/p_i)_{crit}$ ; then:

$$v_e = a = \sqrt{\frac{\gamma p_e}{\rho_e}} = \sqrt{\frac{2\gamma}{\gamma-1} \frac{p_i}{\rho_i} \left(1 - (p_e/p_i)_{crit}^{(\gamma-1)/\gamma}\right)} \quad (A12)$$

Rearranging Eq. (A12) gives:

$$1 - (p_e/p_i)_{crit}^{(\gamma-1)/\gamma} = \frac{\gamma-1}{2} \frac{\rho_i}{\rho_e} \frac{p_e}{p_i} \quad (A13)$$

but

$$\frac{\rho_i}{\rho_e} = (p_i/p_e)^{1/\gamma} \quad (A14)$$

from the isentropic relations used earlier. Substituting Eq. (A14) into Eq. (A13)

$$1 - (p_e/p_i)_{crit}^{(\gamma-1)/\gamma} = \frac{\gamma-1}{2} \frac{(p_e/p_i)_{crit}}{(p_e/p_i)_{crit}^{1/\gamma}} = \frac{\gamma-1}{2} (p_e/p_i)_{crit}^{(\gamma-1)/\gamma} \quad (A15)$$

$$(1 + (\gamma-1)/2) (p_e/p_i)_{crit}^{(\gamma-1)/\gamma} = 1 \quad (A16)$$

and solving for the pressure ratio, we have

$$(p_e/p_i)_{crit} = (2/(\gamma+1))^{\gamma/(\gamma-1)} \quad (A17)$$

Equation (A17) is the expression for the critical pressure ratio. For a  $\gamma = 1.40$ , the critical pressure ratio is 0.5283. When the pressure ratio is less than  $(p_e/p_i)_{crit}$  the flow is choked and the volume flow rate is maximum. Eqs. (A11) and (A17) have been used in the computer programs referenced in this report.

The volume flow rate for the venting apparatus used on our payloads has been measured experimentally. The valves, filters, and orifices are modelled by developing mathematical formulas for their flow characteristics. Originally, this was accomplished from manufacturer's data. However, upon close examination that information was found to be quite dated and it was deemed necessary to experimentally test the apparatus. The numerical information on the valves and filters presented in Table A1 is based upon this empirical data. Leaks are modelled as orifices and are governed by the following equation.



$$m = A_e \sqrt{64.8 p \Delta p}$$

(A18)

From which we see that  $Q \propto \Delta p$ , or that  $\ln Q \propto 0.5 \ln \Delta p$  for an orifice.

Table A1. Valve and Filter Mathematical Models

CIRCLE SEAL Pressure Relief Valves James. Pond & Clark, Inc., Pasadena, CA	
P-243-0.10	
Labeled cracking pressure	0.10 psi
Measured cracking pressure	0.0387 psi
Knee pressure	0.10 psi
Volume flow rate curve:	
$\Delta p < 0.10$	$\ln Q = 10.5789 + 4.7952 \ln \Delta p$
$\Delta p \geq 0.10$	$= 0.9767 + 0.4556 \ln \Delta p$
P7-637-0.50	
Labeled cracking pressure	0.50 psi
Measured cracking pressure	0.3250 psi
Knee pressure	0.59 psi
Volume flow rate curve:	
$\Delta p < 0.59$	$\ln Q = 12.7900 + 17.3978 \ln \Delta p$
$\Delta p \geq 0.59$	$= 3.8647 + 0.4785 \ln \Delta p$
Valve volume flow rate modelled by:	
$Q = \exp(A + B \ln \Delta p)$	
MILLIPORE Filters Millipore Corp., Bedford, MA	
CW-19 Cartridge Filter	
A = -5.6347	
B = 114.9396	
C = -60.0416	
D = 12.9880	
Filter volume flow rate modelled by:	
$Q = A + B(\Delta p) + C(\Delta p)^2 + D(\Delta p)^3$	
Filter length Q multiplier	
31 inch	$Q \times 1.41$
22 inch	$Q \times 1.00$
12 inch	$Q \times 0.50$
RA-2500 Membrane filter 1.2 $\mu$ m pore size	
A = -0.00702	
B = 2.0191	
$A_e$ = Exit area in square inches	
Filter volume flow rate modelled by:	
$Q = [A + B(\Delta p)] A_e$	

The knee pressure listed in Table A1 is that pressure at which the valve bottoms out and its flow area becomes constant. The valve will then begin to act in a manner similar to an orifice. This is reflected in the values of the slopes of the flow curves approximately equalling 0.5. Any discrepancies are probably due to the effects of discharge coefficients which are not directly taken into account here. They are a function of the fluid pressure and the Reynolds number.

A correction factor must be applied to the above numerical data to correct for the fact that the measurements were taken at atmospheric pressure and are being applied at altitude (lower than atmospheric pressure). From the orifice Eq. (A18) we see that  $Q$  is mainly a function of the density:

$$Q = f(\sqrt{\rho \Delta p / \rho}). \quad (A19)$$

Rearranging we have

$$Q = f(\rho^{1/2} / \rho) = f(1/\rho^{1/2}) = f(1/p^{1/2}). \quad (A20)$$

Thus, the volume flow rate is inversely proportional to the square root of the pressure:

$$Q_{atm} \propto 1/p_{atm}^{1/2} \quad Q_i \propto 1/p_i^{1/2}. \quad (A21)$$

Then

$$Q_i / Q_{atm} = (p_{atm} / p_i)^{1/2} \quad (A22)$$

and the low pressure correction is

$$Q_i = Q_{atm} (p_{atm} / p_i)^{1/2} \quad (A23)$$

where  $Q_{atm}$  is the measured volume flow rate at atmospheric conditions. The low pressure correction was included with the compressible flow equations in the computer programs.

A comparison of the computer prediction and the measured results of the test configuration showed that the program was accurate except at the higher altitudes (lower external pressures). Experimenting with the computer program, it was found that an additional correction factor of the form

$$Q_i = Q_{atm} (p_i / p_{atm})^n \quad (A24)$$

(where  $n$  is between 0.20 and 0.30) increases its accuracy. This additional correction factor could possibly incorporate the affects of a discharge coefficient. The total correction factor applied to the measured volume flow rate is:

$$Q_{\text{corr}} = (p_{\text{atm}}/p_i)^{0.50} (p_i/p_{\text{atm}})^{0.25} = (p_{\text{atm}}/p_i)^{0.25} . \quad (\text{A25})$$

The following then, are the operating conditions that are used in the programs developed for the PDP-11/34 computer.

For valves:

$\Delta p < p_c$			$\dot{m}_v = 0$
$\Delta p \geq p_c$	$p_e/p_i > (p_e/p_i)_{\text{crit}}$	$M < 1$ $Q = f(\Delta p)$	$\dot{m}_v = \rho Q Q_{\text{corr}}$
	$p_e/p_i \leq (p_e/p_i)_{\text{crit}}$	$M = 1$ $Q = \text{constant}$ (choked)	$\dot{m}_v = \rho Q_{\text{previous}}$

For filters:

$M < 1$	$Q = f(\Delta p)$	$\dot{m}_f = \rho Q Q_{\text{corr}}$
$M = 1$	$Q = \text{constant}$ (choked)	$\dot{m}_f = \rho Q_{\text{previous}}$

For leaks and orifices:

$M < 1$	$Q = f(\Delta p)$	$\dot{m}_o = \rho Q$
$M = 1$	$Q = \text{constant}$ (choked)	$\dot{m}_o = \rho Q_{\text{previous}}$

From the above, we can see that even though the venting apparatus becomes choked, the MASS flow rates can increase or decrease because the density of the flow can increase or decrease. Only the VOLUME flow rate is affected by choking.

## Appendix B

### Listing and Flowchart of PRESS4.FOR

#### Computer Program PRESS4.FOR

Language:	FORTRAN IV
Computer:	DEC PDP-11/34A
Memory Requirements:	8K Words
Fortran File Size:	21 Blocks
Input File:	FTN30.DAT
Output Files:	FTN31.DAT FTN32.DAT
Major Equations Used:	Equations (7), (A11), (A18), (A25), and those of Table A1.
Integration Technique:	Fourth-order Runge-Kutta process, Eqs. (8) and (9); see also Subroutine RK2 of Reference 4.

```

      PROGRAM PRESS4
C-----PROGRAM PRESS4.FOR
C-----THIS PROGRAM IS AN ATTEMPT TO PREDICT THE INTERNAL PRESSURE OF A
C-----PAYLOAD ON A ROCKET AS IT ASCENDS THROUGH THE ATMOSPHERE. THE
C-----PAYLOAD IS SET UP AS A CHAMBER WITH ATTACHED VENTING VALVES,
C-----FILTERS AND ORIFICES. DOOR LEAKS ARE MODELLED AS ORIFICES. THE
C-----PROGRAM NUMERICALLY INTEGRATES THE DIFFERENTIAL EQUATION THAT
C-----REPRESENTS THE PRESSURE DERIVATIVE.
C-----AUTHOR: C. F. KREBS

      DIMENSION GAS(5),TITLE(20),PREXT(100),PTIME(100)
      REAL MASS,MULT
      DATA QRATE1,QRATE2,QRATEF,QRATEL,RAIL,RAIEF,RAIEL,RAIEVL,RAIEV2,
      Y      DCUEFF,INDEX,I,INDEX,I,MARK/9*0.,0.90,2,0,0/
C-----FORMAT STATEMENTS
9000 FORMAT('0A4')
9100 FORMAT('10,7F10.0')
9101 FORMAT('8F10.0')
9200 FORMAT(/10X,'GAS PROPERTIES:/'
      *      15X,'TYPE:                ',20A4/
      *      15X,'MAIN VOLUME            = ',F10.2,' CU FT'/
      *      15X,'INITIAL PRESSURE       = ',F10.2,' PSI'/
      *      15X,'TEMPERATURE            = ',F10.1,' DEGREES F'/
      *      15X,'GAS CONSTANT           = ',F10.2,' FT-LB/LB-DEG R'/
      *      //)
9201 FORMAT(/10X,'VALVE ONE PROPERTIES:/'
      *      15X,'TYPE:                ',20A4/
9202 FORMAT( 15X,'NUMBER OF RELIEF VALVES = ',F10.0/
      *      15X,'CRACKING PRESSURE      = ',F10.2,' PSI'/
      *      15X,'CURVE CHANGE POINT     = ',F10.2,' PSI'/
      *      15X,'COEFFICIENT 1          = ',F10.3/
      *      15X,'COEFFICIENT 2          = ',F10.3/
      *      15X,'COEFFICIENT 3          = ',F10.3/
      *      15X,'COEFFICIENT 4          = ',F10.3/)
9203 FORMAT(/10X,'VALVE TWO PROPERTIES:/'
      *      15X,'TYPE:                ',20A4/
9204 FORMAT(/10X,'FILTER PROPERTIES:/'
      *      15X,'TYPE:                ',20A4/
9207 FORMAT( 15X,'NUMBER OF FILTERS      = ',F10.0/
      *      15X,'EXIT AREA              = ',F10.5,' SQ IN'/
      *      15X,'COEFFICIENT 1          = ',F10.3/
      *      15X,'COEFFICIENT 2          = ',F10.3/
      *      15X,'COEFFICIENT 3          = ',F10.3/
      *      15X,'COEFFICIENT 4          = ',F10.3/)
9209 FORMAT(/10X,'DOOR LEAK PROPERTIES:/'
      *      15X,'TYPE OF SEAL:         ',20A4/
9210 FORMAT( 15X,'EFFECTIVE AREA         = ',F10.8,' SQ FT'/)
9212 FORMAT(/10X,'CHOKING PROPERTIES:/'
      *      15X,'RATIO OF SPECIFIC HEATS = ',F10.3/
      *      15X,'CRITICAL PRESSURE RATIO = ',F10.4/
      *      15X,'SPEED OF SOUND          = ',F10.1,' FPS'//)
9215 FORMAT(12X,'EXTERNAL  INTERNAL',14X,'INTERNAL',4X,'TOTAL MASS'/
      *      5X,'TIME ',2(' PRESSURE'),3X,'DELTA P',4X,'GAS MASS',
      *      5X,'FLOW RATE',5X,'SECS',6X,'PSI',2(7X,'PSI'),9X,'LRM',
      *      8X,'LBM/SEC'/)
9216 FORMAT(F9.1,2F10.2,F10.3,F13.5,F14.7)
9220 FORMAT(56X,'VALVE ONE',9X,'VALVE TWO',8X,'FILTER ONE',
      *      9X,'LEAK ONE',13X,'P R E S S U R E',19X,4(9X,'FLOW RATE')/
      *      2X,'TIME  EXT  INT  RATIO DIFFR',3X,'MACH  DENSITY ',
      *      4('VOLUME  MASS  ')/2X,'SECS',2(3X,'PSI'),3X,'PE/P1',
      *      ' PSI  NO  LRM/CU FT ',4(' CF/S  LBM/SEC ')/)
9221 FORMAT(F6.1,1X,2F6.2,F7.4,F7.3,F8.3,F9.5,4(F8.4,F10.6))

```

```

C-----TIME REFERENCES
      TIME=0.00
C-----ALLOCATE DATA FILES
      NIN=30
      NOUT=NIN+1
      NOUT2=NOUT+1
C-----INPUT AND OUTPUT OF VITAL INFORMATION
C-----GAS PROPERTIES
      READ(NIN,9000) TITLE
      READ(NIN,9000) GAS
      READ(NIN,9101) VOLUME,VOL,PINT,TEMP,RGAS,GAMMA
      WRITE(NOUT,9000) TITLE
      WRITE(NOUT,9200) GAS,VOLUME,PINT,TEMP,RGAS
      WRITE(NOUT2,9000) TITLE
      WRITE(NOUT2,9220)
C-----VALVE ONE PROPERTIES
      50  READ(NIN,9000) TITLE
          READ(NIN,9101) VALVS1,CRACK1,CHANG1,A1,A2,A3,A4
          WRITE(NOUT,9201) TITLE
          IF (VALVS1.EQ.0.) GO TO 100
          WRITE(NOUT,9202) VALVS1,CRACK1,CHANG1,A1,A2,A3,A4
C-----VALVE TWO PROPERTIES
      100 READ(NIN,9000) TITLE
          READ(NIN,9101) VALVS2,CRACK2,CHANG2,R1,B2,B3,B4
          WRITE(NOUT,9203) TITLE
          IF (VALVS2.EQ.0.) GO TO 110
          WRITE(NOUT,9202) VALVS2,CRACK2,CHANG2,R1,B2,B3,B4
C-----FILLER ONE PROPERTIES
      110 READ(NIN,9000) TITLE
          READ(NIN,9101) FILTRS,AFILT,C1,C2,C3,C4
          WRITE(NOUT,9206) TITLE
          IF (FILTRS.EQ.0.) GO TO 120
          WRITE(NOUT,9207) FILTRS,AFILT,C1,C2,C3,C4
C-----LEAK ONE PROPERTIES
      120 READ(NIN,9000) TITLE
          READ(NIN,9101) ALEAK
          WRITE(NOUT,9209) TITLE
          IF (ALEAK.EQ.0.) GO TO 170
          WRITE(NOUT,9210) ALEAK
C-----INPUT OF EXTERNAL PRESSURE HISTORY
      170 READ(NIN,9101) TIMEND,TSTEP,DIVIDE
          READ(NIN,9100) MAGNIT
          READ(NIN,9101) (PTIME(N),PREXT(N),N=1,MAGNIT)
C-----CONVERSION TO PROPER UNITS
          TEMP=TEMP+459.67
          PINT=PINT+PREXT(1)/144.
          PATM=PREXT(1)
C-----CALCULATION OF INITIAL CONDITIONS
C-----INTERNAL GAS DENSITY
          MULT=RGAS*TEMP/VOLUME
          MASS=PINT*144./MULT
          DENSITY=MASS/VOLUME
C-----PRESSURE DIFFERENTIAL AND PRESSURE RATIO
          PEXT=PREXT(1)/144.
          DELTA=PINT-PEXT
          PRATIO=PEXT/PINT
C-----CRITICAL PRESSURE RATIO
          EXP1=(GAMMA-1.)/GAMMA
          EXP2=1./EXP1
          PRCRIT=(2./(GAMMA+1.))*EXP2

```

```

C-----THROAT VELOCITY AND SPEED OF SOUND
      VMULT=64.348*EXP2
      VEL=1.-PRATIO**EXP1
      VEL=SQRT(VMULT*PINT*144.*VEL/DENSTY)
      VSOUND=1.-PRCRTI**EXP1
      VSOUND=SQRT(VMULT*PINT*144.*VSOUND/DENSTY)
      VMACH=VEL/VSOUND
C#####C
C#####      INITIAL FLOW RATE CONDITIONS      #####C
C#####C
C-----VALVE ONE FLOW RATE CALCULATION
      IF (VALVS1.EQ.0.) GO TO 205
      IF (DELTA.LI.CRACK1) GO TO 205
      IF (DELTA.GI.CHANG1) GO TO 200
      A5=A1
      A6=A2
      GO TO 201
200    A5=A3
      A6=A4
201    RATEV1=EXP(A5+A6*ALOG(DELTA))
      QRATE1=RATEV1/60.*VALVS1
      RATEV1=QRATE1*DENSTY
C-----VALVE TWO FLOW RATE CALCULATION
205    IF (VALVS2.EQ.0.) GO TO 210
      IF (DELTA.LI.CRACK2) GO TO 210
      IF (DELTA.GI.CHANG2) GO TO 206
      B5=B1
      B6=B2
      GO TO 207
206    B5=B3
      B6=B4
207    RATEV2=EXP(B5+B6*ALOG(DELTA))
      RATEV2=RATEV2*MASS/60./VOLUME*VALVS2
      QRATE2=RATEV2/DENSTY
210    RATEV=RATEV1+RATEV2
C-----FILTER FLOW RATE CALCULATION
      IF (FILTRS.EQ.0.) GO TO 220
      RATEF=C1+C2*DELTA+C3*DELTA**2+C4*DELTA**3
      RATEF=RATEF*AFILT*FILTRS
      RATEF=RATEF*MASS/60./VOLUME
      QRATEF=RATEF/DENSTY
C-----ADD IN LEAK CONTRIBUTION IF ANY
220    IF (ALEAK.EQ.0.) GO TO 230
      RATEL=UCOEFF*ALEAK*SQRT(64.348*MASS*DELTA*144./VOLUME)
      QRATEL=RATEL/DENSTY
230    RATE=RATEV+RATEL+RATEF
C-----OUTPUT INITIAL CONDITIONS
300    WRITE(NOUT,9212) GAMMA,PRCRTI,VSOUND
      WRITE(NOUT,9215)
      WRITE(NOUT,9216) TIME,PEXT,PINT,DELTA,MASS,RATE
      WRITE(NOUT,9221) TIME,PEXT,PINT,PRATIO,DELTA,VMACH,DENSTY,
      *      QRATE1,RATEV1,QRATE2,RATEV2,QRATEF,RATEF,
      *      QRATEL,RATEL
C#####C
C#####      INTEGRATION OF DIFFERENTIAL EQUATION      #####C
C#####C
C-----INITIALIZE VARIABLES
      H2=1STEP/2.
      PINT=PINT*144.
      I1=0.
      I2=0.

```

```

      T3=0.
      T4=0.
C-----INTEGRATION LOOP
      500  PRESS=PINT
           TIMES=TIME
           KOUNT=0.
C-----INTEGRATION POINT COUNTER
      540  KOUNT=KOUNT+1
C-----INTERPOLATE TABLE FOR EXTERNAL PRESSURE
      550  IF (TIMES.LE.PTIME(INDEX)) GO TO 560
           INDEX=INDEX+1
           GO TO 550
      560  IF (TIMES.GE.PTIME(INDEX-1)) GO TO 570
           INDEX=INDEX-1
           GO TO 560
      570  IF (INDEX.GT.MAGN1) GO TO 1000
           FRACN=(TIMES-PTIME(INDEX-1))/(PTIME(INDEX)-PTIME(INDEX-1))
           PEXT=PREXT(INDEX-1)+(PREXT(INDEX)-PREXT(INDEX-1))*FRACN
C-----CALCULATE THE INTERNAL GAS MASS & ORATE CORRECTION FACTOR
           MASS=PRESS/MULT
           DENSITY=MASS/VOLUME
           QCURR=SQRT(PAINT/PRESS)
           QCORR=SQRT(QCURR)
C-----CALCULATE THE PRESSURE DIFFERENCE
           KEY=0
           DELTA=(PRESS-PEXT)/144.
           IF (DELTA.LE.0.) KEY=1
           IF (DELTA.LE.0.) DELTA=0.000000
C-----CALCULATE PRESSURE RATIO AND THROAT VELOCITY
           PRATIO=PEXT/PRESS
           VEL=1.-PRATIO**EXP1
           IF (VEL.LT.0.) VEL=0.000000
           VEL=SQRT(VMULT*PRESS*VEL/DENSITY)
           IF (VEL.GT.VSOUND) VEL=VSOUND
           VMACH=VEL/VSOUND
C=====VALVE ONE CALCULATIONS
C-----CHECK WHETHER VALVE ONE IS OPEN OR CLOSED
           IF (VALVS1.EQ.0.) GO TO 580
           IF (DELTA.LT.CRACK1) GO TO 580
C-----VALVE ONE IS OPEN - FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW CONDITION
           IF (VMACH.GE.1.) GO TO 579
           IF (DELTA.GT.CHANG1) GO TO 575
           A5=A1
           A6=A2
           GO TO 576
      575  A5=A3
           A6=A4
      576  QRATE1=EXP(A5+A6*ALOG(DELTA))
           QRATE1=QRATE1/60.*VALVS1*QCORR
C-----CHOKED VALVE - FLOW RATE CALCULATION
      579  RATEV1=QRATE1*DENSITY
           GO TO 585
C-----VALVE ONE IS CLOSED
      580  RATEV1=0.0
C=====VALVE TWO CALCULATIONS
C-----CHECK WHETHER VALVE TWO IS CLOSED OR OPEN
      585  IF (VALVS2.EQ.0.) GO TO 590
           IF (DELTA.LT.CRACK2) GO TO 590

```



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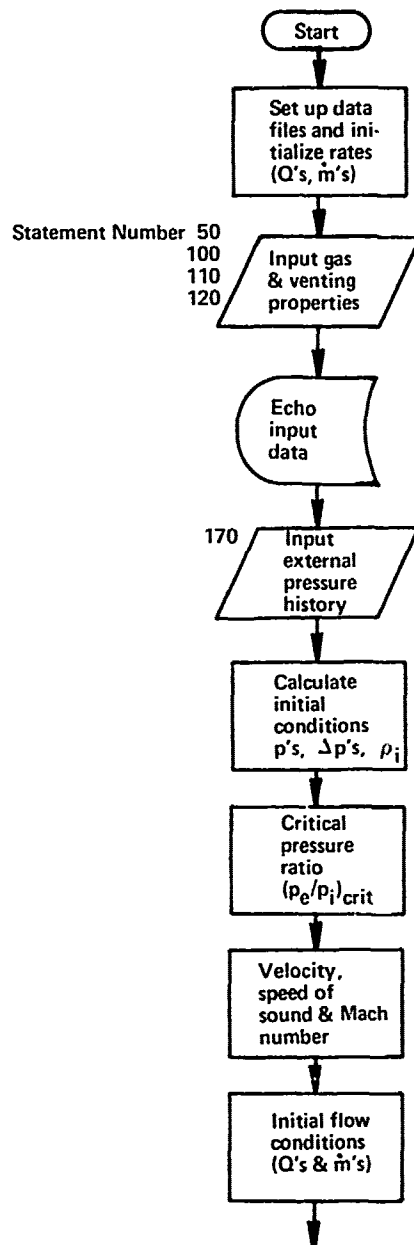
C-----VALVE TWO IS OPEN - FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW CONDITION
      IF (VMACH.GE.1.) GO TO 589
      IF (DELTA.GT.CHANG2) GO TO 586
      R5=R1
      R6=B2
      GO TO 587
586   R5=B3
      R6=B4
587   QRATE2=EXP(R5+B6*ALOG(DELTA))
      QRATE2=QRATE2/60.*VALVS2*QCORR
C-----CHOKED VALVE - FLOW RATE CALCULATION
589   RATEV2=QRATE2*DENS*Y
      GO TO 595
C-----VALVE TWO IS CLOSED
590   RATEV2=0.0
C=====FILTER FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW
595   IF (FILTRS.EQ.0.) GO TO 597
      IF (VMACH.GE.1.) GO TO 596
      QRATEF=C1+C2*DELTA+C3*DELTA**2+C4*DELTA**3
      IF (KEY.EQ.1.) (QRATEF=0.00
      QRATEF=QRATEF*AFILT*FILTRS/60.*QCORR
C-----CHOKED FILTER - FLOW RATE CALCULATION
596   RATEF=QRATEF*DENSITY
C=====ORIFICE FLOW RATE CALCULATIONS - ADD IN LEAK CONTRIBUTION IF ANY
C-----CHECK FOR CHOKED FLOW
597   IF (ALEAK.EQ.0.) GO TO 599
      IF (VMACH.GE.1.) GO TO 598
      RATEL=DCOEFF*ALEAK*SQR(64.348*MASS*DELTA*144./VOLUME)
      QRATEL=RATEL/DENSITY
      GO TO 599
C-----CHOKED CONDITION
598   RATEL=QRATEL*DENSITY
C-----CALCULATE THE TOTAL FLOW RATE AND PRESSURE DERIVATIVE
599   RATE=RATEV1+RATEV2+RATEL+RATEF
      PRADER=-MULT*RATE
C-----PERFORM INTEGRATION CALCULATIONS
600   GO TO (650,700,800,900),KOUNT
650   T1=ISTEP*PRADER
      PRESS=PINT+T1/2.
      TIMES=TIME+H2
      GO TO 540
700   T2=ISTEP*PRADER
      PRESS=PINT+T2/2.
      TIMES=TIME+H2
      GO TO 540
800   T3=ISTEP*PRADER
      PRESS=PINT+T3
      TIMES=TIME+ISTEP
      GO TO 540
900   T4=ISTEP*PRADER
C-----CALCULATE NEW INTERNAL PRESSURE
      KOUNT=0
      PINT=PINT+(T1+2.*T2+2.*T3+T4)/6.
C-----CONTINUE THE INTEGRATION
1000  TIME=TIME+ISTEP
      IF (TIME.GE.TIMEND) GO TO 1500
      LINDEX=LINDEX+1
      RRMARK=LINDEX/DIVIDE

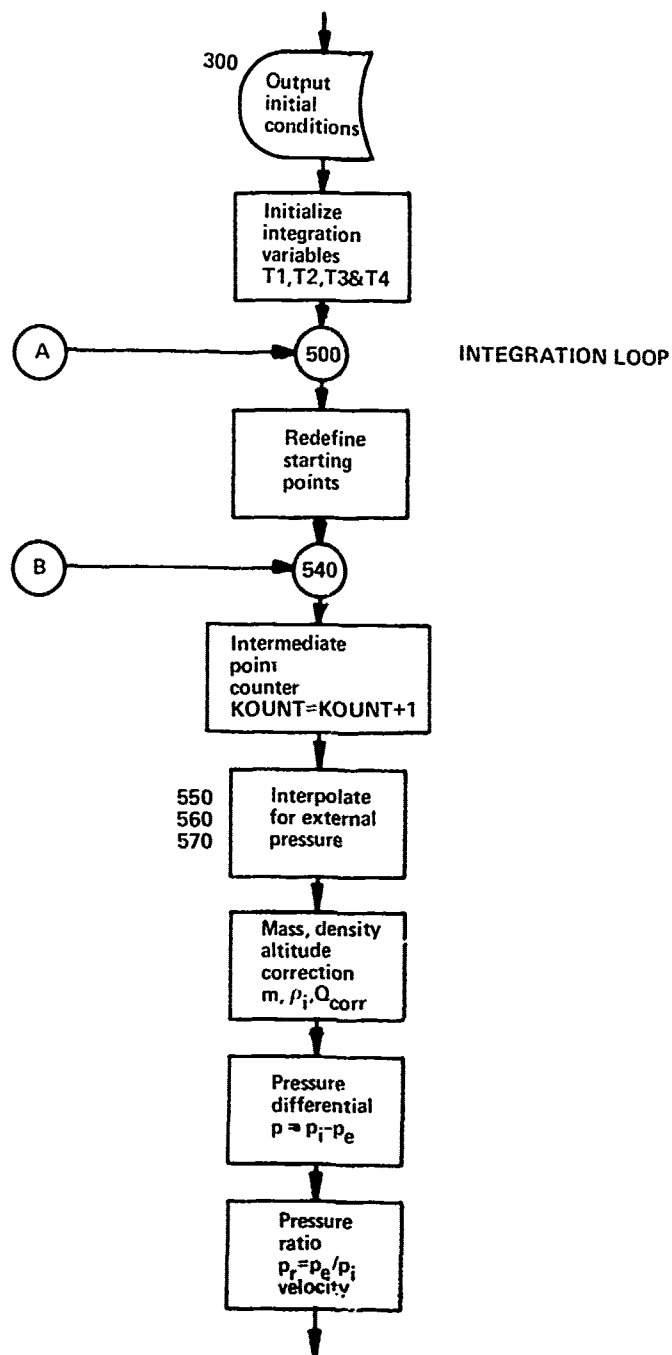
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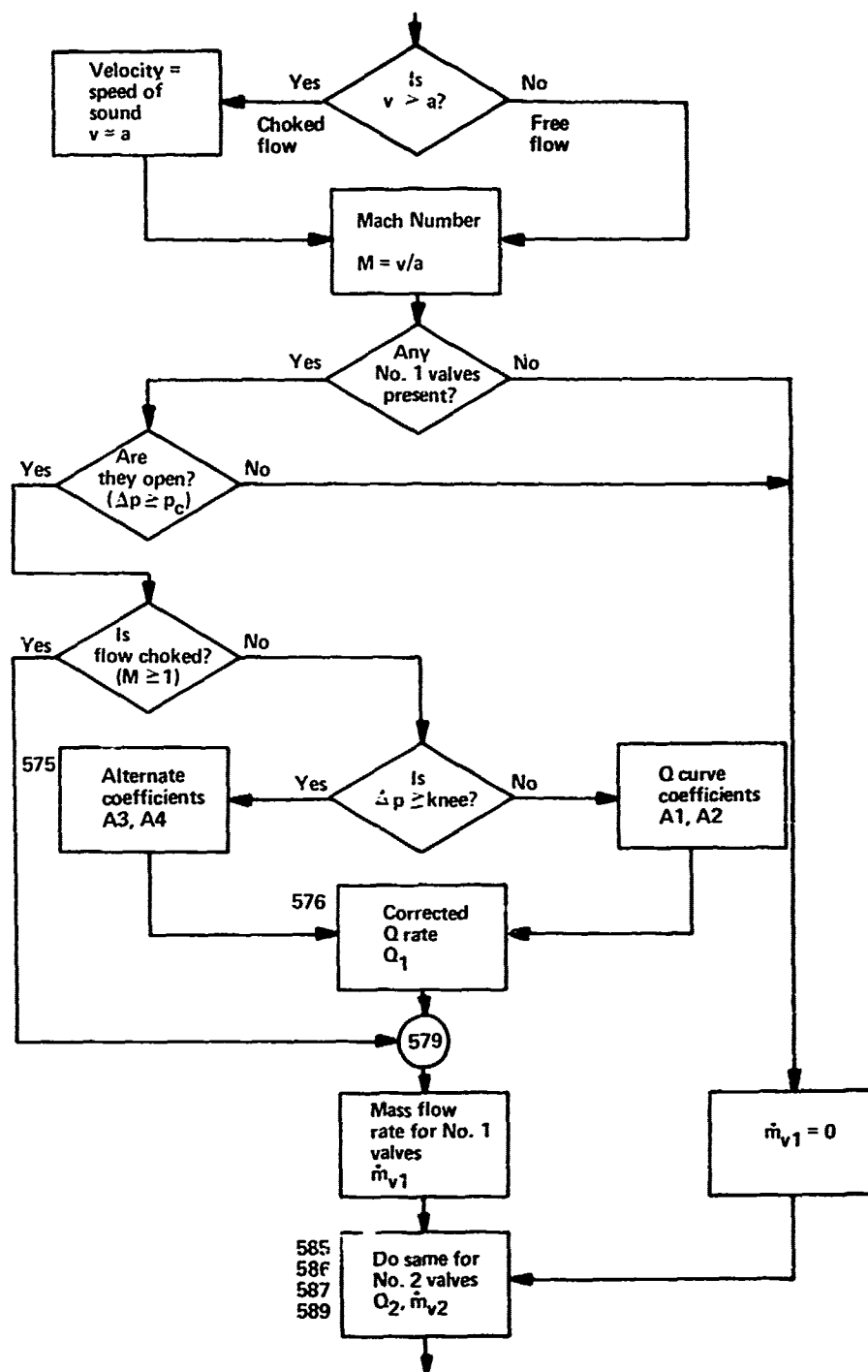
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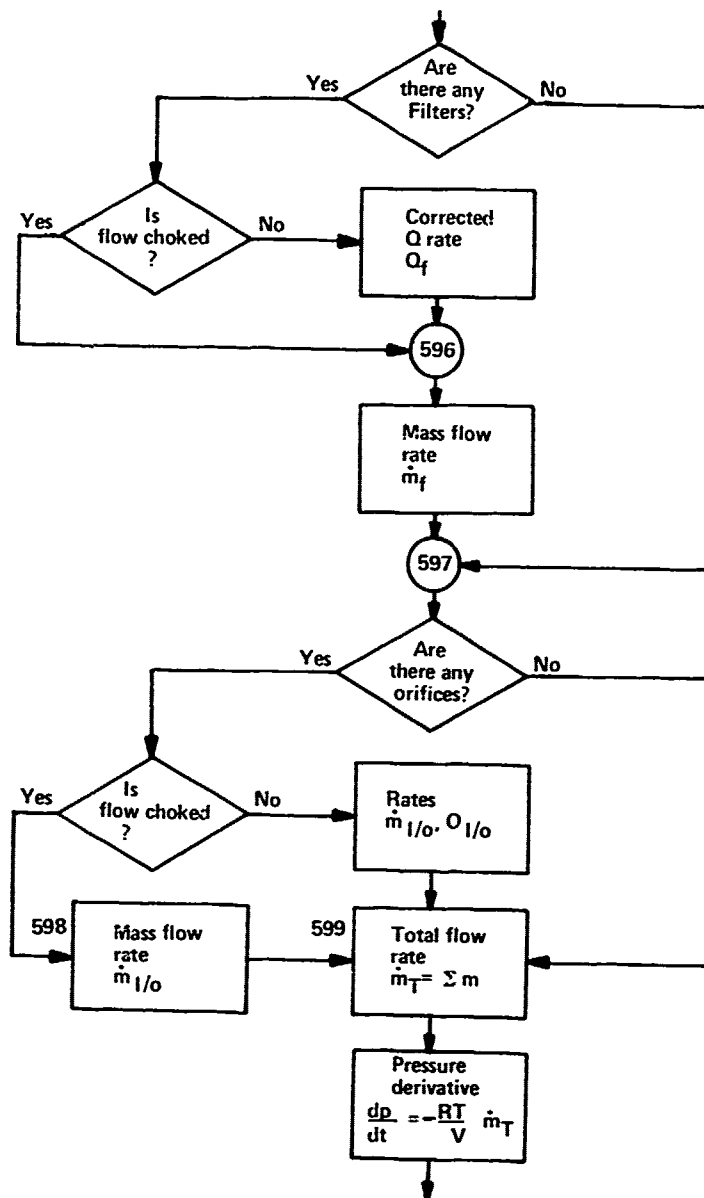
      LMARK=RRMARK
      RMARK=LMARK
      IF (RRMARK.NE.RMARK) GO TO 500
1500  WRITE(7,9216) TIME
      PINT=PINT/144.
      PEXT=PEX1/144.
      WRITE(NOUT,9216) TIME,PEXT,PINT,DELTA,MASS-RATE
      WRITE(NOUT2,9221) TIME,PEXT,PINT,PRATIO,DELTA,VMACH,DENSITY,
*          QRATE1,RATEV1,QRATE2,RATEV2,QRATEF,RATEF,
*          QRATEL,RATEL
      PINT=PINT*144.
      IF (TIME.II.TJMENU) GO TO 500
      STOP 'END OF INTEGRATION'
      END

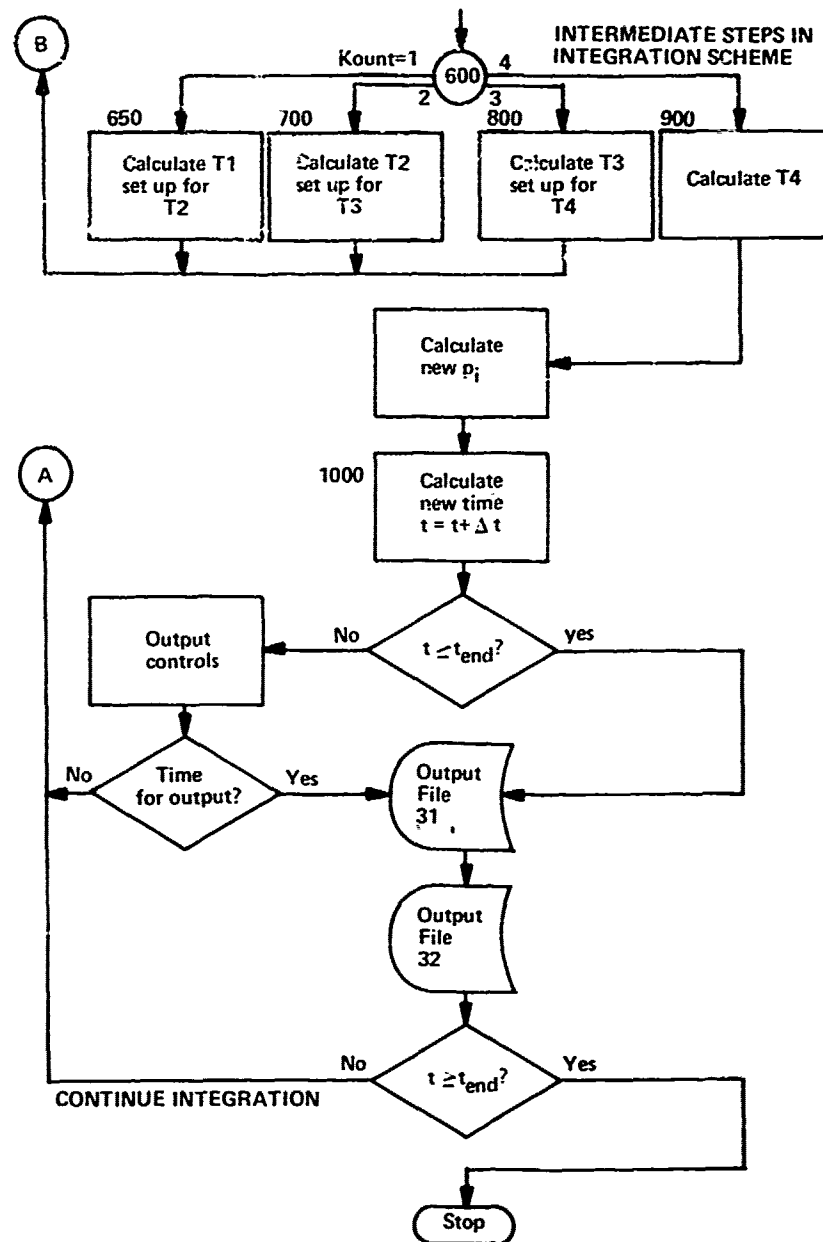
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## Appendix C

### Listing and Flowchart of PRESSM.FOR

#### Computer Program PRESSM.FOR

Language:	FORTRAN IV	
Computer:	DEC PDP-11/34A	
Memory Requirements:	11K Words	
Fortran File Size:	22 Blocks	
Input File:	FTN30. DAT	
Output Files:	FTN31. DAT {	Primary Volume
	FTN32. DAT {	
	FTN33. DAT {	Secondary Volume
	FTN34. DAT }	
Subroutines:	RKGS	(integration routine)
	PREQNS	(called by RKGS)



```

C-----PROGRAM PRESSM.FOR
C-----THIS IS AN ATTEMPT TO PREDICT THE INTERNAL PRESSURE OF A
C-----SOUNDING ROCKET AS IT ASCENDS THROUGH THE ATMOSPHERE.
C-----THE PROGRAM CALCULATES THE INTERNAL PRESSURE HISTORY OF A
C-----SET OF MULTIPLE INTERCONNECTED CHAMBERS. AT PRESENT THE PROGRAM
C-----ALLOWS ONLY TWO VOLUMES. THE PROGRAM INTEGRATES THE DIFFERENTIAL
C-----EQUATIONS NUMERICALLY USING A FOURTH-ORDER RUNGE-KUTTA SCHEME.
C-----THE INTEGRATION IS DONE IN THE "RKGS" SUBROUTINE CALLED BY THIS
C-----PROGRAM. THE DIFFERENTIAL EQUATIONS ARE EVALUATED AT VARIOUS
C-----TIMES BY THE "PREONS" SUBROUTINE WHICH IS CALLED BY "RKGS."
C-----AUTHOR: C. M. KREBS
      DIMENSION AUX(8*2),LIMITS(5),PRESS(2),PREFEED(2)
      DIMENSION CAS(5),TIME(20)
      COMMON /INPUTS/ VALV51,CRACK1,CHANG1,B1,B2,B3,B4,
* VALV52,CRACK2,CHANG2,B1,B2,B3,B4,
* VALV53,CRACK3,CHANG3,B1,B2,B3,B4,
* VALV54,CRACK4,CHANG4,B1,B2,B3,B4,
* TIME51,TIME12,TIME13,TIME14,TIME15,TIME16,TIME17,TIME18,TIME19,TIME20
      COMMON /OUTPUT/ TIME,PIN1,PEXT,RA1,VEL1A1,DENS1,MASS1,VEL1,
* VMACH1,RATE1,RATE2,RATE3,RATE4,RATE5,RATE6,RATE7,RATE8,
* ORATE1,ORATE2,ORATE3,PIN2,PRAT1,PRAT2,PRAT3,DELTA2,
* DELTA3,DENS2,MASS2,VEL2,VEL3,VMACH2,VMACH3,
* RATE2,RATE3,RATE4,RATE5,RATE6,RATE7,RATE8,
* ORATE4,ORATE5,ORATE6
      COMMON /REFEED/ VOL1,VOL2,MUL1,MUL2,ORATE1,EXFL,VSOUND,
* PEXT(100),TIME(100),INDEX,DOEFF,MAGN1
      REAL LIMITS,MASS1,MASS2,MUL1,MUL2
      EXTERNAL PREONS
      DATA ORATE1,ORATE2,ORATE3,ORATE4,ORATE5,ORATE6,ORATE7,ORATE8,
* RATE1,RATE2,RATE3,RATE4,RATE5,RATE6,RATE7,RATE8,
* RATE9,RATE10,RATE11,DOEFF,INDEX,INDEX,LMARK/19*0.0,90,
* 2*0.0/
C-----FORMAT STATEMENTS
9000 FORMAT(20A4)
9100 FORMAT(110,7F10.0)
9101 FORMAT(8I10.0)
9200 FORMAT(/10X,'GAS PROPERTIES:/'
* 15X,'TYPE: ' /5A4/
* 15X,'MAIN VOLUME ' /F10.2/ CU FT//
* 15X,'SECOND VOLUME ' /F10.2/ CU FT//
* 15X,'INITIAL PRESSURE ' /F10.2/ PSI//
* 15X,'TEMPERATURE ' /F10.1/ DEGREES F//
* 15X,'GAS CONSTANT ' /F10.2/ BTU/LB-DEG R/
* //)
9201 FORMAT(/10X,'VALVE ONE PROPERTIES:/'
* 15X,'TYPE: ' /20A4/
9202 FORMAT( 15X,'NUMBER OF RELIEF VALVES ' /F10.0/
* 15X,'CRACKING PRESSURE ' /F10.2/ PSI//
* 15X,'CURVE CHANGE POINT ' /F10.2/ PSI//
* 15X,'COEFFICIENT 1 ' /F10.3/
* 15X,'COEFFICIENT 2 ' /F10.3/
* 15X,'COEFFICIENT 3 ' /F10.3/
* 15X,'COEFFICIENT 4 ' /F10.3/
9203 FORMAT(/10X,'VALVE TWO PROPERTIES:/'
* 15X,'TYPE: ' /20A4/
9204 FORMAT(/10X,'VALVE THREE PROPERTIES:/'
* 15X,'TYPE: ' /20A4/
9205 FORMAT(/10X,'VALVE FOUR PROPERTIES:/'
* 15X,'TYPE: ' /20A4/

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9206 FORMAT(10X,'FILTER ONE PROPERTIES: /
*      15X,'TYPE:              ',20A4)
9207 FORMAT(15X,'NUMBER OF FILTERS      - ',F10.0/
*      15X,'EXT. AREA              - ',F10.5,' SQ IN' /
*      15X,'COEFFICIENT 1          = ',F10.3/
*      15X,'COEFFICIENT 2          = ',F10.3/
*      15X,'COEFFICIENT 3          = ',F10.3/
*      15X,'COEFFICIENT 4          = ',F10.3/)
9208 FORMAT(10X,'FILTER TWO PROPERTIES: /
*      15X,'TYPE:              ',20A4)
9209 FORMAT(10X,'DOOR LEAK ONE PROPERTIES: /
*      15X,'TYPE OF SEAL:         ',20A4)
9210 FORMAT(15X,'EFFECTIVE AREA      - ',F10.9,' SQ FT' /)
9211 FORMAT(10X,'DOOR LEAK TWO PROPERTIES: /
*      15X,'TYPE OF SEAL:         ',20A4)
9212 FORMAT(10X,'CHOFFING PROPERTIES: /
*      15X,'RATIO OF SPECIFIC HEATS - ',F10.3/
*      15X,'CRITICAL PRESSURE RATIO = ',F10.4/
*      15X,'SPEED OF SOUND          = ',F10.1,' FPS' / /)
9213 FORMAT( MAIN VOLUME CALCULATIONS' /)
9214 FORMAT( SECONDARY VOLUME CALCULATIONS' /)
9215 FORMAT(2X,'EXTERNAL' INTERNAL',14X,'INTERNAL',4X,'TOTAL MASS' /
*      5X,'TIME',2X,'PRESSURE',3X,'DELTA P',4X,'GAS MASS' /
*      5X,'FLOW RATE',5X,'SECS',6X,'PSI',2(2X,'PSI'),9X,'LRM',
*      8X,'LRM/SEC' /)
9216 FORMAT(F9.1,2F10.2,F10.3,F13.5,F14.7)
9217 FORMAT(19X,'PRESSURE',11X,'PRESSURE DIFF',5X,'TOTAL MASS' /
*      5X,'TIME',6X,'EXT. MAIN VOL. SEC. VOL.',5X,'MAIN',
*      5X,'EXT.',6X,'FLOW RATE',5X,'SECS',6X,'PSI',4(2X,'PSI'),
*      7X,'LRM/SEC' /)
9218 FORMAT(F9.1,3F10.2,2F10.3,F14.7)
9219 FORMAT(56X,'VALVE ONE',9X,'VALVE TWO',8X,'FILTER ONE',
*      9X,'LEAK ONE',13X,'PRESSURE',10X,4(9X,'FLOW RATE') /
*      7X,'TIME',EXI INT. RATIO DUEK',3X,'MACH DENSITY',
*      4('VOLUME MASS'),2X,'SECS',2(3X,'PSI'),3X,'PE/P1',
*      PSI NO LRM/CU FT',4('CF/S LRM/SEC' /))
9220 FORMAT(F6.1,1X,2F6.2,F7.4,F7.3,F8.3,F9.5,4(F8.4,F10.6))
9221 FORMAT(9X,'MAIN VOL. REFERENCE',4X,'EXTERNAL REFERENCE',
*      14X,'VALVE THREE',7X,'VALVE FOUR',8X,'FILTER TWO',
*      9X,'LEAK TWO',11X,'PRESSURE',14X,'PRESSURE',15X,
*      4(9X,'FLOW RATE'),2X,'TIME',2(3X,'RATIO DIFFR. MACH'),
*      2X,'DENSITY',3('VOLUME MASS'),('VOLUME MASS'),2X,
*      'SECS P1/P2 PSI NO PE/P2 PSI NO LRM/CU',
*      'FT',4('CF/S LRM/SEC' /))
9222 FORMAT(F6.1,2(F7.3),F9.5,4(F8.4,F10.6))
C----- TIME REFERENCES
TIME=0.00
C-----ALLOCATE DATA FILES
NIN=30
NOUT=NIN+1
NOUT2=NOUT+1
NOUT3=NOUT+2
NOUT4=NOUT+3
C-----INPUT AND OUTPUT OF VITAL INFORMATION
C----- GAS PROPERTIES
READ(NIN,9000) TITLE
READ(NIN,9000) GAS
READ(NIN,9101) VOL1,VOL2,PINI,TEMP,RGAS,GAMMA
WRITE(NOUT,9000) TITLE
WRITE(NOUT,9200) GAS,VOL1,VOL2,PINI,TEMP,RGAS

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WRITE(NOUT2,9000) TITLE
WRITE(NOUT2,9213)
WRITE(NOUT2,9220)
IF (VOL2.EQ.0.) GO TO 50
WRITE(NOUT3,9000) TITLE
WRITE(NOUT4,9000) TITLE
WRITE(NOUT4,9214)
WRITE(NOUT4,9222)
C-----MAIN VOLUME PRESSURE SYSTEM
C-----VALVE ONE PROPERTIES
100 READ(NIN,9000) TITLE
READ(NIN,9101) VALVS1,CRACK1,CHANG1,A1,A2,A3,A4
WRITE(NOUT1,9201) TITLE
IF (VALVS1.EQ.0.) GO TO 100
WRITE(NOUT1,9202) VALVS1,CRACK1,CHANG1,A1-A2,A3,A4
C-----VALVE TWO PROPERTIES
110 READ(NIN,9000) TITLE
READ(NIN,9101) VALVS2,CRACK2,CHANG2,B1,B2,B3,B4
WRITE(NOUT1,9203) TITLE
IF (VALVS2.EQ.0.) GO TO 110
WRITE(NOUT1,9202) VALVS2,CRACK2,CHANG2,B1,B2,B3,B4
C-----FILTER ONE PROPERTIES
110 READ(NIN,9000) TITLE
READ(NIN,9101) FILTS1,AFILT1,E1,E2,E3,E4
WRITE(NOUT1,9204) TITLE
IF (FILTS1.EQ.0.) GO TO 120
WRITE(NOUT1,9207) FILTS1,AFILT1,E1,E2,E3,E4
C-----LEAK ONE PROPERTIES
120 READ(NIN,9000) TITLE
READ(NIN,9101) ALEAK1
WRITE(NOUT1,9209) TITLE
IF (ALEAK1.EQ.0.) GO TO 130
WRITE(NOUT1,9210) ALEAK1
C-----SECOND VOLUME PRESSURE SYSTEM
130 IF (VOL2.EQ.0.) GO TO 170
C-----VALVE THREE PROPERTIES
READ(NIN,9000) TITLE
READ(NIN,9101) VALVS3,CRACK3,CHANG3,C1,C2,C3,C4
WRITE(NOUT3,9204) TITLE
IF (VALVS3.EQ.0.) GO TO 140
WRITE(NOUT3,9202) VALVS3,CRACK3,CHANG3,C1,C2,C3,C4
C-----VALVE FOUR PROPERTIES
140 READ(NIN,9000) TITLE
READ(NIN,9101) VALVS4,CRACK4,CHANG4,D1,D2,D3,D4
WRITE(NOUT3,9205) TITLE
IF (VALVS4.EQ.0.) GO TO 150
WRITE(NOUT3,9202) VALVS4,CRACK4,CHANG4,D1,D2,D3,D4
C-----FILTER TWO PROPERTIES
150 READ(NIN,9000) TITLE
READ(NIN,9101) FILTS2,AFILT2,F1,F2,F3,F4
WRITE(NOUT3,9208) TITLE
IF (FILTS2.EQ.0.) GO TO 160
WRITE(NOUT3,9207) FILTS2,AFILT2,F1,F2,F3,F4
C-----LEAK TWO PROPERTIES
160 READ(NIN,9000) TITLE
READ(NIN,9101) ALEAK2
WRITE(NOUT3,9211) TITLE
IF (ALEAK2.EQ.0.) GO TO 170
WRITE(NOUT3,9210) ALEAK2

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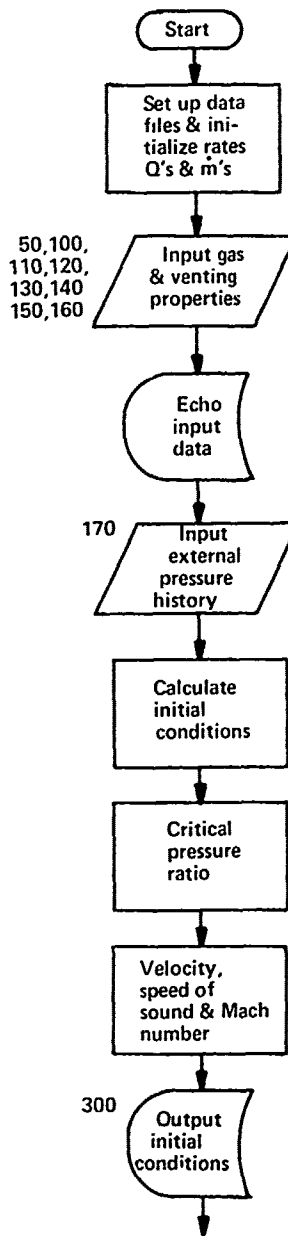
C-----INPUT OF EXTERNAL PRESSURE HISTORY
170 READ(NIN,9101) TIMEN 1 2, DIVIDE, LIMITS(4)
    READ(NIN,9100) MAGC
    READ(NIN,9101) (PI, 'REXI(N), N=1, MAGN11)
C-----CONVERSION TO PROPER UNITS
    TEMP=TEMP+459.67
    PINI=PINI+PREXT('144.
C-----CALCULATION OF INITIAL CONDITIONS
C-----MAIN VOLUME
C-----INTERNAL GAS DENSITY
    MU11=RGAS*TEMP/VOL1
    MASS1=PINI*144./MU11
    DENS1=MASS1/VOL1
C-----PRESSURE DIFFERENTIAL AND PRESSURE RATIO
    PEX1=PREXT(1)/144.
    DELTA1=PINI-PEX1
    PRAT1=PEX1/PINI
C-----CRITICAL PRESSURE RATIO
    EXP1=(GAMMA-1.)/GAMMA
    EXP2=1./EXP1
    PRCRIT=(2./(GAMMA+1.))*EXP2
C-----THROAT VELOCITY AND SPEED OF SOUND
    VMUL1=64.348*EXP1
    VEL1=1.-PRAT1**EXP1
    VEL1=SQRT(VMUL1*PINI*144.*VEL1/DENS1)
    VSOUND1=1.-PRAT1**EXP1
    VSOUND1=SQRT(VMUL1*PINI*144.*VSOUND1/DENS1)
    VMACH1=VEL1/VSOUND1
C-----SETUP VOLUME
    IF (VOL2.EQ.0.) GO TO 300
    MU12=RGAS*TEMP/VOL2
    MASS2=PINI*144./MU12
    DENS2=MASS2/VOL2
    DELTA2=PINI-PINI
    DELTA3=PINI-PEX1
    PRAT2=PINI/PINI
    PRAT3=PEX1/PINI
    VEL2=1.-PRAT2**EXP1
    VEL2=SQRT(VMUL1*PINI*144.*VEL2/DENS2)
    VMACH2=VEL2/VSOUND1
C-----OUTPUT INITIAL CONDITIONS
300 WRITE(NOUT,9212) GAMMA,PRCRIT,VSOUND1
    WRITE(NOUT,9213)
    WRITE(NOUT,9215)
    WRITE(NOUT,9216) TIME,PEX1,PINI,DELTA1,MASS1,RATE1
    WRITE(NOUT,9221) TIME,PEX1,PINI,PRAT1,DELTA1,VMACH1,DENS1,
    * RATE1,RATEV1,RATE2,RATEV2,RATEF1,RATEF1,
    * RATE1,RATE1
    IF (VOL2.EQ.0.) GO TO 400
    WRITE(NOUT,9214)
    WRITE(NOUT,9217)
    WRITE(NOUT,9218) TIME,PEX1,PINI-PINI,DELTA2,DELTA3,RATE3
    WRITE(NOUT,9223) TIME,PRAT2,DELTA2,VMACH2,PRAT3,DELTA3,VMACH3,
    * DENS2,RATE3,RATEV3,RATE4,RATEV4,RATEF2,
    * RATE12,PRAT12,RATE12
C-----SETUP FOR INTEGRATION LOOP
C-----INITIAL VALUES
400 PRESS(1)=PINI*144.
    PRESS(2)=PRESS(1)

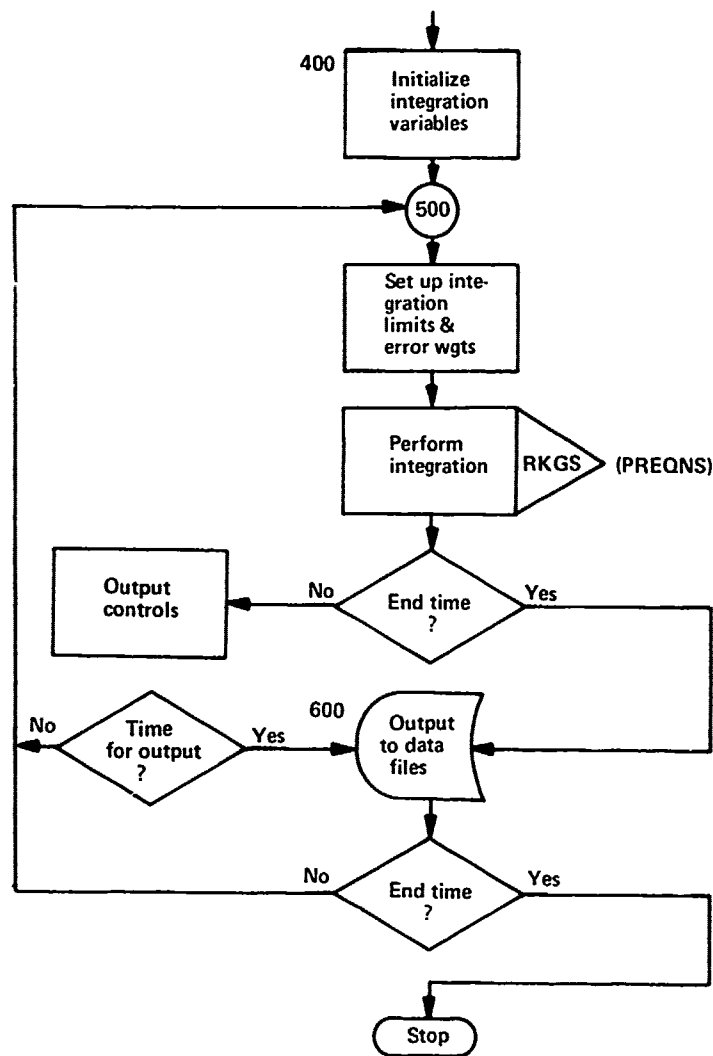
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1 - - - INTEGRATION LOOP
500  LIMITS(1)=TIME
    LIMITS(2)=TIME+1STEP
    LIMITS(3)=1STEP
C---- RESET ERROR WEIGHTS
    PREDER(1)=0.50
    PREDER(2)=0.50
C---- CALL INTEGRATION ROUTINE
    CALL RKGS(LIMITS,PRESS,PREDER,2,NSECT,PREDNS,AUX)
    IF (TIME.GE.TIMEND) GO TO 600
    IINDEX=LINDEX+1
    RRMARK=IINDEX/DIVIDE
    LMARK=RRMARK
    KMARK=LMARK
    IF (RRMARK.NE.LMARK) GO TO 500
600  WRITE(7,9216) TIME
    WRITE(NOUT,9216) TIME,PEXT,PINI1,DELTA1,MASS1,RATE1
    WRITE(NOUT2,9221) TIME,PEXT,PINI1,PRAT1,DELTA1,VMACH1,DENS1,
*      QRATE1,RATEV1,QRATE2,RATEV2,QRATE1,RATEF1,
*      QRATE1,RATEF1
    IF (VOL2.EQ.0.) GO TO 700
    WRITE(NOUT3,9218) TIME,PEXT,PINI1,PINI2,DELTA2,DELTA3,RAT
    WRITE(NOUT4,9223) TIME,PRAT2,DELTA2,VMACH2,PRAT3,DELTA3,VMACH3,
*      DENS2,QRATE3,RATEV3,QRATE4,RATEV4,QRATE2,
*      RATEF2,QRATE2,RATEF2
700  IF (TIME.LT.TIMEND) GO TO 500
    STOP 'END OF INTEGRATION'
END

```





#### Subroutine RKGS. FOR

Modified RKGS routine of Reference 4; called by main program to integrate the differential equations.

The following lines have been modified to eliminate the use of the external output routine:

RKGS 1050  
RFGS 1530  
RKGS 2280  
RKGS 2570

Integration Technique: Self-starting fourth-order Runge-Kutta solution of a system of first-order ordinary differential equations.

#### Subroutine PREQNS. FOR

Called by RKGS subroutine to evaluate the differential equations during integration process.

Major Equations Used: Equations (12), (13), (14), (A11), (A18), (A25), and those of Table A1.



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SUBROUTINE PREQNS(TIMEIN,PRESS,PREDER)
C-----PREQNS.FOR
C-----THIS SUBROUTINE IS USED WITH THE "PRESSM" PROGRAM TO PREDICT THE
C-----INTERNAL PRESSURE OF A SOUNDING ROCKET PAYLOAD. IT CALCULATES
C-----THE FLOW CHARACTERISTICS OF THE PRESSURE RELIEF VALVES, FILTERS AND
C-----ORIFICES USING THE EMPIRICALLY DERIVED FLOW CURVES. IT EVALUATES
C-----THE DIFFERENTIAL EQUATIONS FOR THE INTEGRATION SUBROUTINE "RKGS"
C-----WHICH IS CALLED FROM THE MAIN PROGRAM.
C-----AUTHOR: C. F. KERS
      DIMENSION PRESS(2),PREDER(2)
      COMMON /INPUTS/ VALVS1,CRACK1,CHANG1,A1,A2,A3,A4,
      * VALVS2,CRACK2,CHANG2,B1,B2,B3,B4,
      * VALVS3,CRACK3,CHANG3,C1,C2,C3,C4,
      * VALVS4,CRACK4,CHANG4,D1,D2,D3,D4,
      * FILTS1,AFILT1,F1,E2,E3,F4,ALEAK1,
      * FILTS2,AFILT2,F1,F2,F3,F4,ALEAK2
      COMMON /OUTPUT/ TIME,PINT1,PEXT,PRAT1,DELTA1,DENS1,MASS1,VEL1,
      * VMACH1,RATE1,RATE01,RATE02,RATEF1,RATE1,QRATE1,
      * QRATE2,QRATE1,QRATE1,PINT2,PRAT2,PRAT3,DELTA2,
      * DELTA3,DENS2,MASS2,VEL2,VEL3,VMACH2,VMACH3,
      * RATE2,RATE3,RATE03,RATE04,RATEF2,RATE12,QRATE3,
      * QRATE4,QRATE2,QRATE2
      COMMON /REFERS/ VOL1,VOL2,MUL1,MUL2,VMUL1,EXP1,VSSOUND,
      * PREX1(100),PTIME(100),INDEX,DCUEFF,MAGN11
      REAL MASS1,MASS2,MUL1,MUL2
C-----TRANSFER THE TIME
      TIME=TIMEIN
      TIMES=TIME
C-----TRANSFER THE INTERNAL PRESSURES
      PRESS1=PRESS(1)
      PRESS2=PRESS(2)
      PINT1=PRESS(1)/144.
      PINT2=PRESS(2)/144.
C-----INTERPOLATE TABLE FOR EXTERNAL PRESSURE
      100 IF (TIMES.LE.PTIME(INDEX)) GO TO 110
      INDEX=INDEX+1
      GO TO 100
      110 IF (TIMES.GE.PTIME(INDEX-1)) GO TO 120
      INDEX=INDEX-1
      GO TO 110
      120 IF (INDEX.GT.MAGN11) STOP 'INDEX TOO LARGE'
      FRACN=(TIMES-PTIME(INDEX-1))/(PTIME(INDEX)-PTIME(INDEX-1))
      PEXT=PREX1(INDEX-1)+(PREX1(INDEX)-PREX1(INDEX-1))*FRACN
C-----*****C
C-----*****C      INNER VOLUME CALCULATIONS      *****C
C-----*****C
      IF (VOL2.EQ.0.) GO TO 800
C-----CALCULATE GAS PROPERTIES
      MASS2=PRESS2/MUL2
      DENS2=MASS2/VOL2
C-----CALCULATE THE ORATE CORRECTION FACTOR
      QCORR2=SQRT(PREX1(1)/PRESS2)
      QORR2=SQRT(QCORR2)
C-----CALCULATE THE PRESSURE DIFFERENCES
      KEY3=
      DELTA2=(PRESS2-PRESS1)/144.
      DELTA3=(PRESS2-PEXT)/144.
      IF (DELTA3.LE.0.) KEY3=1
      IF (DELTA2.LE.0.) DELTA2=0.000000
      IF (DELTA3.LE.0.) DELTA3=0.000000

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C-----CALCULATE PRESSURE RATIOS AND THROAT VELOCITIES
    PKAT2=PRESS1/PRESS2
    PRAT3=PEXT/PRESS2
    VEL2=1.-PRAT2**EXP1
    IF (VEL2.LE.0.) VEL2=0.000000
    VEL2=SQRT(VMULT*PRESS2*VEL2/DENS2)
    VEL3=1.-PKAT3**EXP1
    IF (VEL3.LE.0.) VEL3=0.000000
    VEL3=SQRT(VMULT*PRESS2*VEL3/DENS2)
    IF (VEL2.GT.VSOUND) VEL2=VSOUND
    IF (VEL3.GT.VSOUND) VEL3=VSOUND
    VMACH2=VEL2/VSOUND
    VMACH3=VEL3/VSOUND

C=====VALVE THREE FLOW CALCULATIONS
C-----CHECK WHETHER VALVE THREE IS OPEN OR CLOSED
    IF (VALVS3.EQ.0.) GO TO 240
    IF (DELTA2.LT.CRACK3) GO TO 240
C-----VALVE THREE IS OPEN - FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW CONDITION
    IF (VMACH2.GE.1.) GO TO 230
    IF (DELTA2.GT.CHANG3) GO TO 210
    C5=C1
    C6=C2
    GO TO 220
210  C5=C3
    C6=C4
220  QRATE3=EXP(C5+C6*ALOG(DELTA2))
    QRATE3=QRATE3/60.*VALVS3*RCORR2
C-----CHOKED VALVE - FLOW RATE CALCULATION
230  RATEV3=QRATE3*DENS2
    GO TO 300
C-----VALVE THREE IS CLOSED
240  RATEV3=0.0
C=====VALVE FOUR FLOW CALCULATIONS
C-----CHECK WHETHER VALVE FOUR IS CLOSED OR OPEN
300  IF (VALVS4.EQ.0.) GO TO 340
    IF (DELTA2.LT.CRACK4) GO TO 340
C-----VALVE FOUR IS OPEN - FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW CONDITION
    IF (VMACH2.GE.1.) GO TO 330
    IF (DELTA2.GT.CHANG4) GO TO 310
    D5=D1
    D6=D2
    GO TO 320
310  D5=D3
    D6=D4
320  QRATE4=EXP(D5+D6*ALOG(DELTA2))
    QRATE4=QRATE4/60.*VALVS4*RCORR2
C-----CHOKED VALVE - FLOW RATE CALCULATION
330  RATEV4=QRATE4*DENS2
    GO TO 400
C-----VALVE FOUR IS CLOSED
340  RATEV4=0.0
C-----TOTAL VALVE FLOW RATE
400  RATE2=RATEV3+RATEV4
C=====FILTER TWO FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW
    IF (FILTS2.EQ.0.) GO TO 610
    IF (VMACH3.GE.1.) GO TO 510

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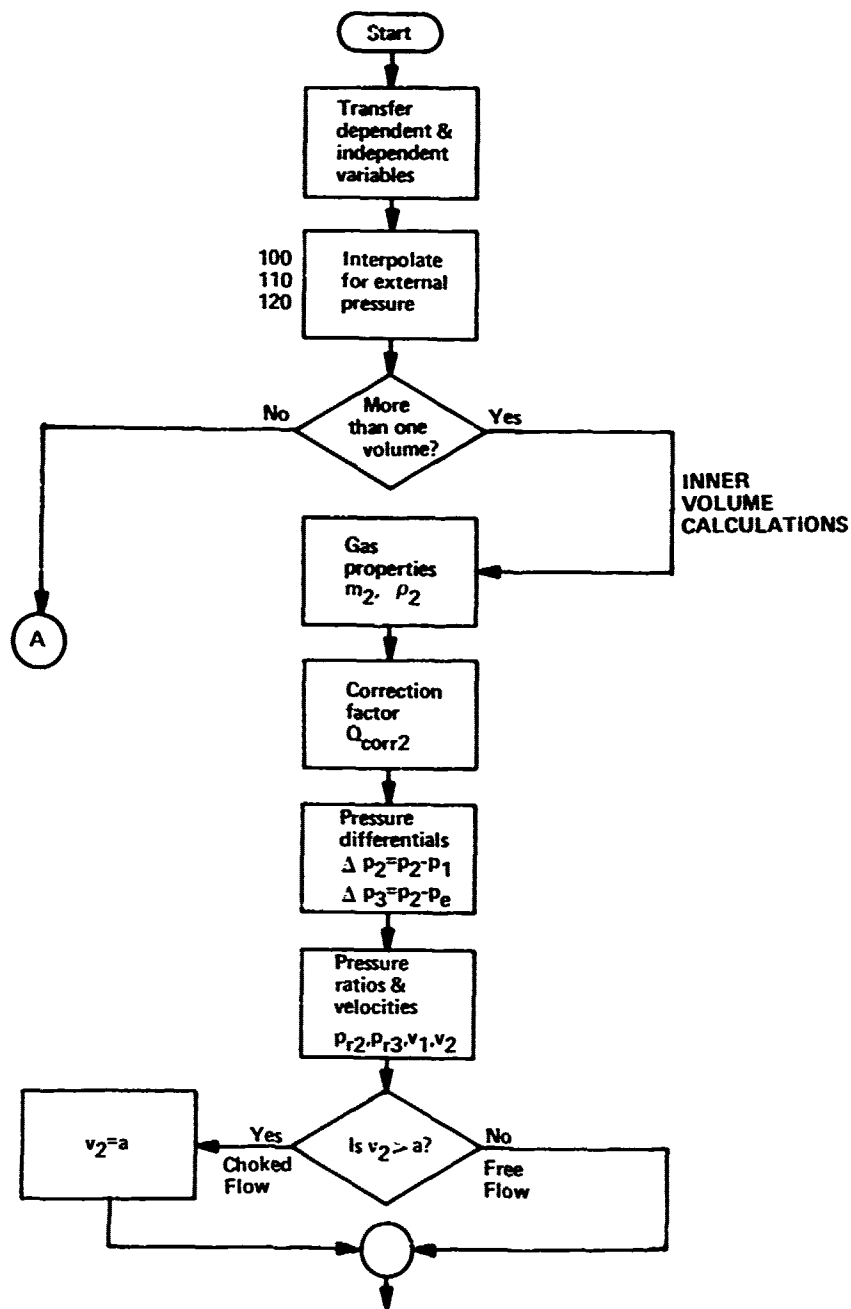
      QRATF2=F1+F2*DELTA3+F3*DELTA3**2+F4*DELTA3**3
      IF (KEY3.EQ.1) QRATF2=0.00
      QRATF2=QRATF2*AFILT2*FILTS2/60.*QCORN2
C-----CHOKED FILTER - FLOW RATE CALCULATION
      S10  RATEF2=QRATF2*DENS2
C=====ORIFICE TWO FLOW CALCULATION - ADD IN LEAK CONTRIBUTION IF ANY
C-----CHECK FOR CHOKED FLOW
      610  IF (ALEAK2.EQ.0.) GO TO 700
           IF (VMACH3.GE.1.) GO TO 620
           RATEL2=DCOEFF*ALEAK2*SQR1(64.348*DENS2*DELTA3*144.)
           QRATL2=RATEL2/DENS2
           GO TO 700
C-----CHOKED CONDITION
      620  RATEL2=QRATL2*DENS2
C-----CALCULATE THE TOTAL FLOW RATE AND PRESSURE DERIVATIVE
      700  RATEF3=RATE2+RATEL2+RATEF2
      800  PREDER(2)=-MULT2*RATE3
C=====*****C
C=====      OUTER VOLUME CALCULATIONS      *****C
C=====*****C
C-----CALCULATE GAS PROPERTIES
      MASS1=PRESS1/MULT1
      DENS1=MASS1/VOL1
C-----CALCULATE THE QRATE CORRECTION FACTOR
      QCORR1=SQR1(PREXT(1)/PRESS1)
      QCORR1=SQR1(QCORR1)
C-----CALCULATE THE PRESSURE DIFFERENCE
      KEY1=0
      DELTA1=(PRESS1-PEXT)/144.
      IF (DELTA1.LE.0.) KEY1=1
      IF (DELTA1.LE.0.) DELTA1=0.000000
C-----CALCULATE PRESSURE RATIO AND THROAT VELOCITY
      PRAT1=PEXT/PRESS1
      PEX1=PEXT/144.
      VEL1=1.-PRAT1**EXP1
      IF (VEL1.LE.0.) VEL1=0.000000
      VEL1=SQR1(VMULT*PRESS1*VEL1/DENS1)
      IF (VEL1.GT.VSOUND) VEL1=VSOUND
      VMACH1=VEL1/VSOUND
C=====VALVE ONE FLOW CALCULATIONS
C-----CHECK WHETHER VALVE ONE IS OPEN OR CLOSED
      IF (VALVS1.EQ.0.) GO TO 1040
      IF (DELTA1.LT.CRACK1) GO TO 1040
C-----VALVE ONE IS OPEN - FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW CONDITION
      IF (VMACH1.GE.1.) GO TO 1030
      IF (DELTA1.GT.CHANG1) GO TO 1030
      A5=A1
      A6=A2
      GO TO 1020
      1010  A5=A3
           A6=A4
      1020  QRATE1=EXP(A5+A6*ALOG(DELTA1))
           QRATE1=QRATE1/60.*VALVS1*QCORR1
C-----CHOKED VALVE - FLOW RATE CALCULATION
      1030  RATEV1=QRATE1*DENS1
           GO TO 1100
C-----VALVE ONE IS CLOSED
      1040  RATEV1=0.0
C=====VALVE TWO FLOW CALCULATIONS

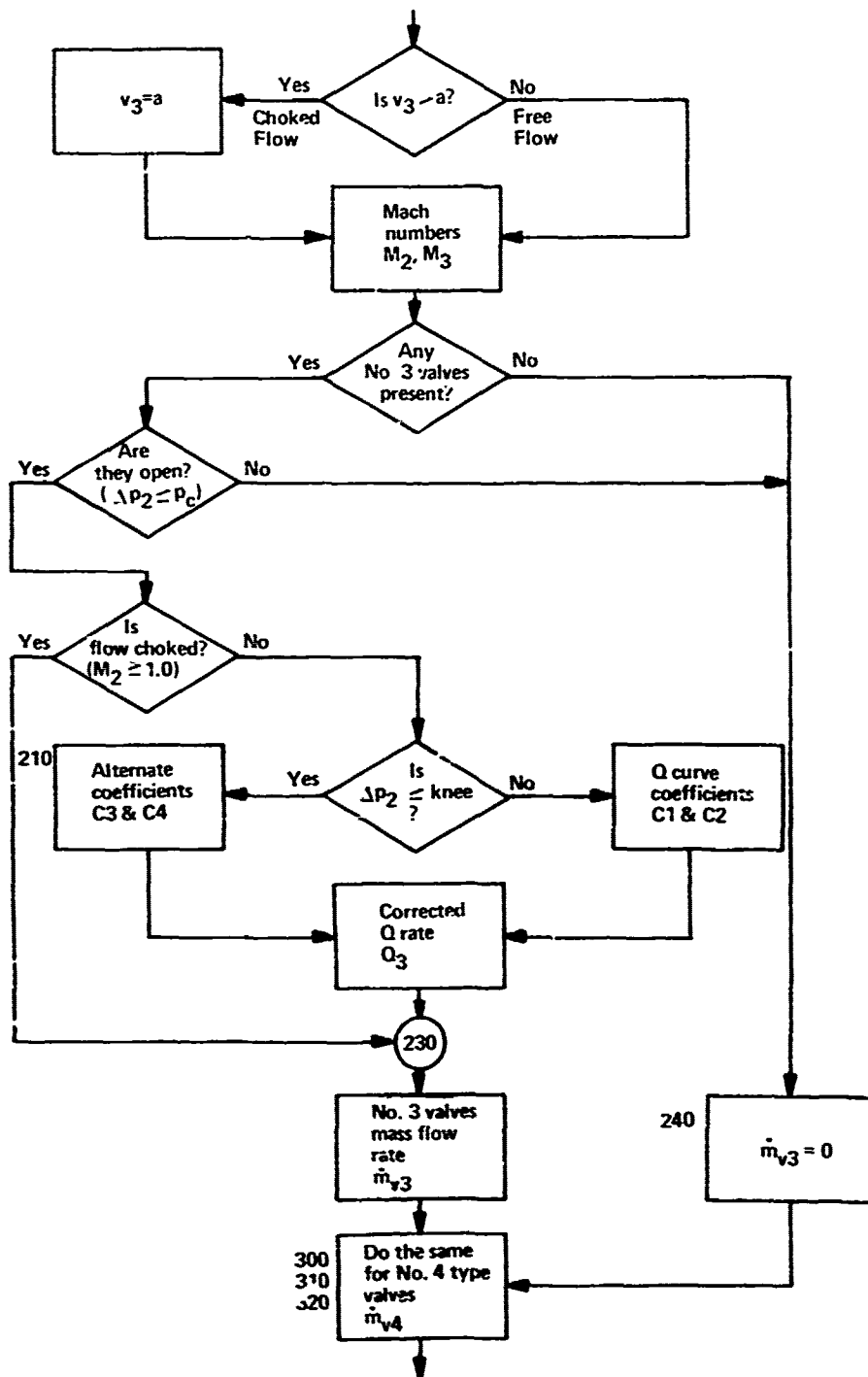
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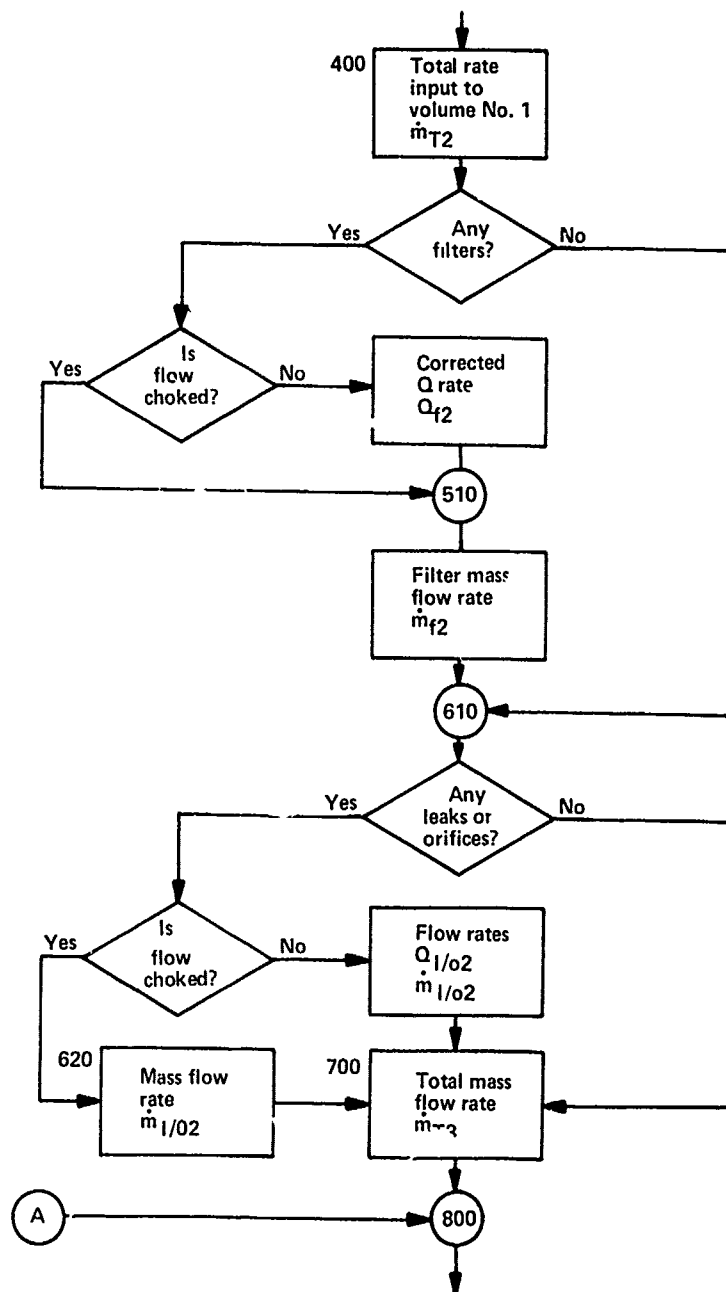
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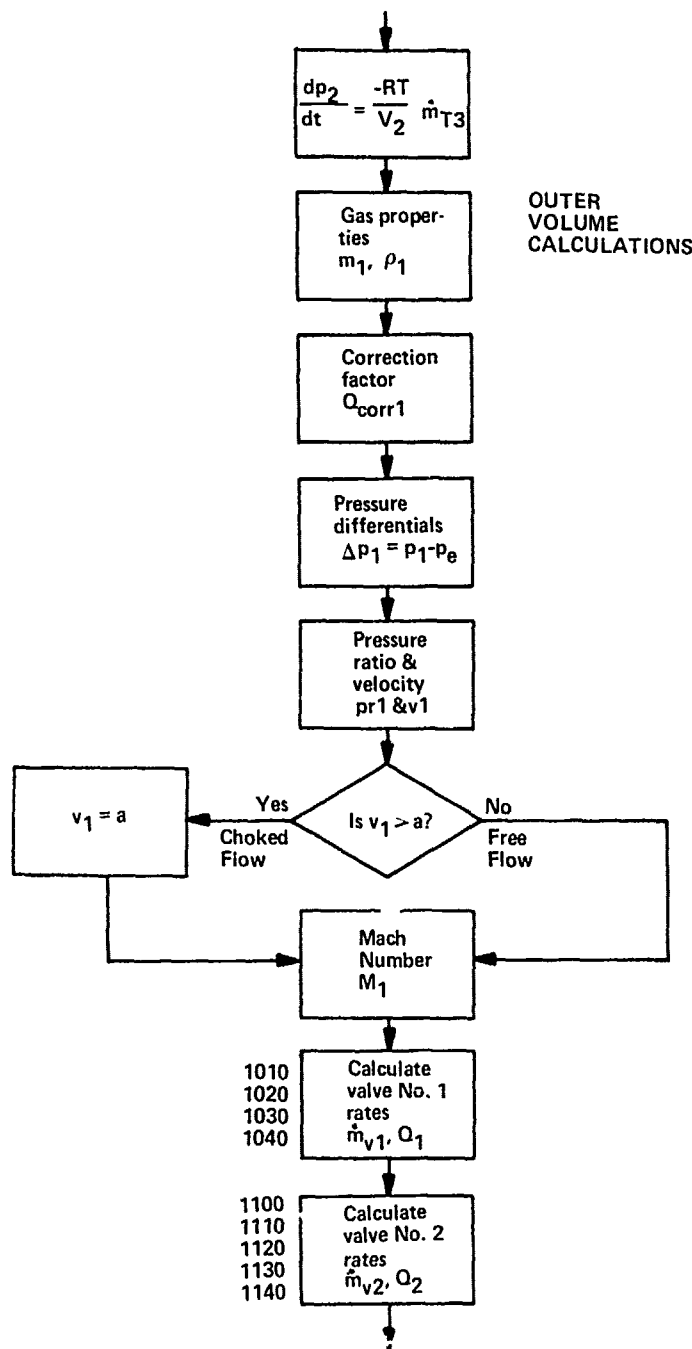
C-----CHECK WHETHER VALVE TWO IS CLOSED OR OPEN
1100  IF (VALVS2.EQ.0.) GO TO 1140
      IF (DELTA1.LT.CRACK2) GO TO 1140
C-----VALVE TWO IS OPEN - FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW CONDITION
      IF (VMACH1.GE.1.) GO TO 1130
      IF (DELTA1.GT.CHANG2) GO TO 1110
      R5=R1
      R6=R2
      GO TO 1120
1110  R5=R3
      R6=R4
1120  QRATE2=EXP(R5+R6*ALOG(DELTA1))
      QRATE2=QRATE2/60.*VALVS2*QCORR1
C-----CHOKED VALVE - FLOW RATE CALCULATION
1130  RATEV2=QRATE2*DENS1
      GO TO 1200
C-----VALVE TWO IS CLOSED
1140  RATEV2=0.0
C=====FILTER ONE FLOW RATE CALCULATION
C-----CHECK FOR CHOKED FLOW
1200  IF (FILTS1.EQ.0.) GO TO 1410
      IF (VMACH1.GE.1.) GO TO 1310
      QRATF1=E1+E2*DELTA1+E3*DELTA1**2+E4*DELTA1**3
      IF (KEY1.EQ.1) QRATF1=0.00
      QRATF1=QRATF1*AFILT1*FILTS1/60.*QCORR1
C-----CHOKED FILTER - FLOW RATE CALCULATION
1310  RATEF1=QRATF1*DENS1
C=====ORIFICE ONE FLOW RATE CALCULATION - ADD IN LEAK CONTRIBUTION IF ANY
C-----CHECK FOR CHOKED FLOW
1410  IF (ALEAK1.EQ.0.) GO TO 1500
      IF (VMACH1.GE.1.) GO TO 1420
      RATEL1=DCOEFF*ALEAK1*SQRT(64.348*DENS1*DELTA1*144.)
      QRATL1=RATEL1/DENS1
      GO TO 1500
C-----CHOKED CONDITION
1420  RATEL1=QRATL1*DENS1
C-----CALCULATE THE TOTAL FLOW RATE AND PRESSURE DERIVATIVE
1500  RATE1=RATEV1+RATEV2+RATEL1+RATEF1
      PREDER(1)=-MULT1*(RATE1-RATE2)
      RETURN
      END

```

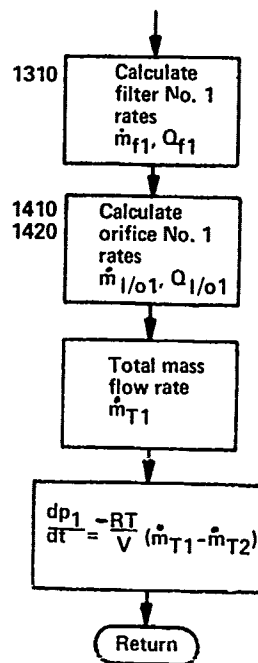












## Appendix D

### Sample Input and Output Data Files

#### Format for Input Data File FTN30.DAT

Line	Format	
1	20A4	Title
2	5A4	Gas type
3	6F10.0	Volume #1, volume #2, initial pressure, initial temperature, gas constant, ratio of specific heats
4	20A4	Valve type #1
5	7F10.0	Number of valves, cracking pressure, knee pressure, curve coefficients A & B (below knee pressure), curve coefficients C & D (above knee pressure)
6	20A4	Valve type #2
7	7F10.0	Same as line 5 except for valve type #2
8	20A4	Filter type
9	6F10.0	Number of filters, filter area/multiplier (for RA-2500 is exit area; for CW-19 is length multiplier) curve coefficients A, B, C, & D
10	20A4	Leak/orifice title
11	F10.0	Effective area of leak or orifice

12	4F10.0	Ending time of calculations, timestep = 0.01 seconds, print interval multiplier = 100., accuracy requirement = 0.001
13	I10	Number of entries to follow in external pressure table
14	8F10.0	Time, external pressure

Notes: For valves, filters, and orifices not present include a title but leave numerical data line blank.

In line 12, the timestep and print interval multiplier.  
determine printout time:  $100 \times 0.01 = 1$  second printout.

In line 14, 4 pairs per line, repeating if necessary.

For PRESSM.FOR, repeat lines 4 through 11 for second volume with primary volume data first and secondary volume data following (see IRBS Payload input file).

#### Units for Input Data File

Gas volume	cubic feet
Initial pressure	pounds per square inch
Initial temperature	degrees F
Gas constant	foot-pounds per pound-degree R
Valve cracking & knee pressure	pounds per square inch
Filter area	square inches
Leak area	square feet
End time	seconds
External pressure table:	
time	seconds
pressure	pounds per square foot

Sample Input Data File (FTN30.DAT)  
for ZIP Payload - PRESS4.FOR

IP PAYLOAD INTERNAL PRESSURE HISTORY  
MIRRORED

5.80 0.12 35.0 55.20 1.400  
CIRCLE SEAL P-249 0.10 PSI MARKED CRACKING PRESSURE  
6. 0.0387 0.10 10.8789 4.7952 0.9767 0.4956  
CIRCLE SEAL P7-637 0.50 PSI MARKED CRACKING PRESSURE  
0. 0.325 0.59 12.7900 17.3978 3.8647 0.4786  
MILLIPORE KA 1.2 MICROMETER PORE SIZE  
2. 0.11045 -0.007017 2.018104  
PERFECT SEAL -- NO LEAK

100.	0.01	100.	0.001
1.0	1827.7	1.0	1826.1
2.0	1799.8	5.0	1781.6
3.0	1711.1	9.0	1678.6
4.0	1557.1	13.0	1509.0
5.0	1346.5	17.0	1287.9
6.0	1104.6	21.0	1042.1
7.0	854.4	25.0	792.7
8.0	614.0	29.0	557.5
9.0	401.1	33.0	355.4
10.0	238.3	37.0	205.9
11.0	127.4	41.0	106.7
12.0	59.8	45.0	48.5
13.0	34.8	49.0	19.6
14.0	9.4	53.0	7.3
15.0	3.3	57.0	2.5
16.0	1.0	61.0	0.7
17.0	0.2	65.0	0.2
18.0	0.05	69.0	0.0
19.0			
20.0			
21.0			
22.0			
23.0			
24.0			
25.0			
26.0			
27.0			
28.0			
29.0			
30.0			
31.0			
32.0			
33.0			
34.0			
35.0			
36.0			
37.0			
38.0			
39.0			
40.0			
41.0			
42.0			
43.0			
44.0			
45.0			
46.0			
47.0			
48.0			
49.0			
50.0			
51.0			
52.0			
53.0			
54.0			
55.0			
56.0			
57.0			
58.0			
59.0			
60.0			
61.0			
62.0			
63.0			
64.0			
65.0			
66.0			
67.0			
68.0			
69.0			
70.0			
71.0			
72.0			
73.0			
74.0			
75.0			
76.0			
77.0			
78.0			
79.0			
80.0			
81.0			
82.0			
83.0			
84.0			
85.0			
86.0			
87.0			
88.0			
89.0			
90.0			
91.0			
92.0			
93.0			
94.0			
95.0			
96.0			
97.0			
98.0			
99.0			
100.0			

Sample Input Data File (FTN30.DAT)  
for IRBS Payload-PRESSM.FOR

IRBS PAYLOAD INTERNAL PRESSURE HISTORY

AIR

46.80 0.1777 0.50 70.0 53.35 1.400  
CIRCLE SEAL P7-637 0.50 PSI MARKED CRACKING PRESSURE  
3. 0.325 0.59 12.7900 17.3978 3.8647 0.4786  
NO SECOND VALVE TYPE PRESENT

NO FILTERS PRESENT

PERFECT SEAL -- NO LEAKS

CIRCLE SEAL P-249 0.10 PSI MARKED CRACKING PRESSURE  
2. 0.0387 0.10 10.8789 4.7952 0.9767 0.4956  
NO SECOND VALVE PRESENT

NO FILTERS PRESENT

DOOR LEAK DUE TO SEAM SEAL

0.000042

100.	0.01	100.	0.001
89			
0.0	1827.7	1.0	1827.7
4.0	1798.8	5.0	1785.4
8.0	1723.7	9.0	1695.5
12.0	1589.6	13.0	1547.9
16.0	1402.5	17.0	1348.8
20.0	1178.8	21.0	1121.3
24.0	947.05	25.0	889.07
28.0	715.94	29.0	659.67
32.0	498.10	33.0	447.64
36.0	314.45	37.0	276.25
40.0	180.08	41.0	153.95
44.0	91.890	45.0	76.198
48.0	41.468	49.0	33.300
52.0	16.354	53.0	12.708
56.0	5.7511	57.0	4.3639
60.0	1.6404	61.0	1.3554
64.0	0.5213	65.0	0.3754
68.0	0.1323	69.0	0.0911
72.0	0.0269	73.0	0.0173
76.0	0.0046	77.0	0.0030
80.0	0.0009	81.0	0.0001
100.0	0.0000	150.0	0.0000
360.0	0.0000		

2.0	6.0	10.0	14.0	18.0	22.0	26.0	30.0	34.0	38.0	42.0	46.0	50.0	54.0	58.0	62.0	66.0	70.0	74.0	78.0	82.0	200.0
1816.7	1768.2	1663.9	1502.1	1292.8	1063.6	830.89	604.40	400.17	241.40	130.62	62.720	26.506	9.8087	3.2927	0.9910	0.2685	0.0617	0.0111	0.0020	0.0000	0.0000
3.0	7.0	11.0	15.0	19.0	23.0	27.0	31.0	35.0	39.0	43.0	47.0	51.0	55.0	59.0	63.0	67.0	71.0	75.0	79.0	90.0	350.0
1809.8	1747.7	1628.7	1453.9	1236.0	1005.5	773.17	550.43	355.76	209.09	109.96	51.207	20.907	7.5328	2.4401	0.7203	0.1897	0.0411	0.0072	0.0013	0.0000	0.0000

Sample Output Data File (FTN31.DAT)  
for ZIP Payload - PRESS4.FOR

ZIP PAYLOAD INTERNAL PRESSURE HISTORY

GAS PROPERTIES:

TYPE: NITROGEN  
MAIN VOLUME = 6.80 CU FT  
INITIAL PRESSURE = 0.12 PSI  
TEMPERATURE = 35.0 DEGREES F  
GAS CONSTANT = 55.20 FT-LB/LB-DEG R

VALVE ONE PROPERTIES:

TYPE: CIRCLE SEAL P-249 0.10 PSI MARKED  
NUMBER OF RELIEF VALVES = 6, CRACKING PRESSURE  
CRACKING PRESSURE = 0.04 PSI  
CURVE CHANGE POINT = 0.10 PSI  
COEFFICIENT 1 = 10.979  
COEFFICIENT 2 = 4.795  
COEFFICIENT 3 = 0.977  
COEFFICIENT 4 = 0.496

VALVE TWO PROPERTIES:

TYPE: CIRCLE SEAL P7-637 0.50 PSI MARKED

FILTER PROPERTIES:

TYPE: MILLIPORE RA 1.2 MICROMETER PORE SIZE  
NUMBER OF FILTERS = 2, CRACKING PRESSURE  
EXIT AREA = 0.11045 SQ IN  
COEFFICIENT 1 = -0.007  
COEFFICIENT 2 = 2.018  
COEFFICIENT 3 = 0.000  
COEFFICIENT 4 = 0.000

DOOR LEAK PROPERTIES:

TYPE OF SEAL: PERFECT SEAL -- NO LEAK

CHOKING PROPERTIES:

RATIO OF SPECIFIC HEATS = 1.400  
CRITICAL PRESSURE RATIO = 0.5283  
SPEED OF SOUND = 1012.4 FPS

TIME SECS	EXTERNAL PRESSURE PSI	INTERNAL PRESSURE PSI	DELTA P PSI	INTERNAL GAS MASS LRM	TOTAL MASS FLOW RATE LRM/SEC
0.0	12.69	12.81	0.120	0.45946	0.0063326
1.0	12.68	12.75	0.066	0.45712	0.0008095
2.0	12.65	12.72	0.072	0.45606	0.0012052
3.0	12.59	12.67	0.081	0.45423	0.0021200
4.0	12.50	12.59	0.088	0.45136	0.0030970
5.0	12.39	12.48	0.093	0.44751	0.0040261
6.0	12.25	12.34	0.098	0.44267	0.0049980
7.0	12.08	12.19	0.108	0.43702	0.0057598

8.0	11.88	12.02	0.134	0.43092	0.0063605
9.0	11.66	11.83	0.171	0.42414	0.0070972
10.0	11.40	11.62	0.214	0.41662	0.0078531
11.0	11.12	11.39	0.256	0.40834	0.0086235
12.0	10.81	11.14	0.322	0.39933	0.0093387
13.0	10.48	10.86	0.385	0.38961	0.0100314
14.0	10.12	10.58	0.453	0.37923	0.0106656
15.0	9.74	10.27	0.525	0.36826	0.0112374
16.0	9.35	9.95	0.598	0.35676	0.0117218
17.0	8.94	9.62	0.672	0.34482	0.0121226
18.0	8.53	9.27	0.747	0.33252	0.0124483
19.0	8.10	8.92	0.821	0.31994	0.0126894
20.0	7.67	8.57	0.895	0.30716	0.0128552
21.0	7.24	8.21	0.969	0.29424	0.0129607
22.0	6.80	7.84	1.043	0.28126	0.0130073
23.0	6.37	7.48	1.115	0.26825	0.0129894
24.0	5.93	7.12	1.186	0.25530	0.0129185
25.0	5.50	6.76	1.256	0.24244	0.0127962
26.0	5.08	6.41	1.324	0.22973	0.012624
27.0	4.67	6.06	1.389	0.21721	0.0124050
28.0	4.26	5.71	1.451	0.20494	0.0121463
29.0	3.87	5.38	1.509	0.19294	0.0118442
30.0	3.49	5.05	1.563	0.18127	0.0115091
31.0	3.13	4.74	1.611	0.16995	0.0111377
32.0	2.79	4.43	1.649	0.15902	0.0107225
33.0	2.47	4.14	1.674	0.14853	0.0102657
34.0	2.17	3.86	1.689	0.13851	0.0097862
35.0	1.90	3.60	1.694	0.12897	0.0092904
36.0	1.65	3.35	1.692	0.12001	0.0086471
37.0	1.43	3.11	1.684	0.11166	0.0080459
38.0	1.23	2.90	1.670	0.10390	0.0074866
39.0	1.05	2.70	1.651	0.09668	0.0069661
40.0	0.88	2.51	1.624	0.08996	0.0064818
41.0	0.74	2.33	1.593	0.08370	0.0060312
42.0	0.62	2.17	1.558	0.07788	0.0056119
43.0	0.51	2.02	1.512	0.07247	0.0052218
44.0	0.42	1.88	1.465	0.06743	0.0048587
45.0	0.34	1.75	1.413	0.06274	0.0045210
46.0	0.27	1.63	1.357	0.05838	0.0042067
47.0	0.22	1.51	1.298	0.05432	0.0039142
48.0	0.17	1.41	1.237	0.05055	0.0036421
49.0	0.14	1.31	1.175	0.04707	0.0033889
50.0	0.11	1.22	1.113	0.04377	0.0031533
51.0	0.08	1.14	1.051	0.04072	0.0029341
52.0	0.07	1.06	0.991	0.03789	0.0027301
53.0	0.05	0.98	0.932	0.03526	0.0025403
54.0	0.04	0.91	0.876	0.03280	0.0023637
55.0	0.03	0.85	0.821	0.03052	0.0021994
56.0	0.02	0.79	0.769	0.02840	0.0020465
57.0	0.02	0.74	0.720	0.02643	0.0019042
58.0	0.01	0.69	0.673	0.02459	0.0017718
59.0	0.01	0.64	0.628	0.02288	0.0016486
60.0	0.01	0.59	0.587	0.02129	0.0015340
61.0	0.00	0.55	0.548	0.01981	0.0014274
62.0	0.00	0.51	0.511	0.01843	0.0013282
63.0	0.00	0.48	0.476	0.01715	0.001235
64.0	0.00	0.45	0.444	0.01596	0.0011499
65.0	0.00	0.41	0.413	0.01485	0.0010700
66.0	0.00	0.39	0.385	0.01382	0.0009954
67.0	0.00	0.36	0.358	0.01285	0.0009264

68.0	0.00	0.33	0.333	0.01196	0.0008620
69.0	0.00	0.31	0.310	0.01113	0.0008020
70.0	0.00	0.29	0.289	0.01036	0.0007463
71.0	0.00	0.27	0.269	0.00964	0.0006944
72.0	0.00	0.25	0.250	0.00897	0.0006461
73.0	0.00	0.23	0.233	0.00834	0.0006012
74.0	0.00	0.22	0.216	0.00776	0.0005594
75.0	0.00	0.20	0.201	0.00722	0.0005205
76.0	0.00	0.19	0.187	0.00672	0.0004843
77.0	0.00	0.17	0.174	0.00625	0.0004507
78.0	0.00	0.16	0.162	0.00582	0.0004193
79.0	0.00	0.15	0.151	0.00542	0.0003902
80.0	0.00	0.14	0.141	0.00504	0.0003631
81.0	0.00	0.13	0.131	0.00469	0.0003378
82.0	0.00	0.12	0.122	0.00436	0.0003143
83.0	0.00	0.11	0.113	0.00406	0.0002925
84.0	0.00	0.11	0.105	0.00378	0.0002721
85.0	0.00	0.10	0.098	0.00351	0.0002532
86.0	0.00	0.09	0.091	0.00327	0.0002356
87.0	0.00	0.08	0.085	0.00304	0.0002192
88.0	0.00	0.08	0.079	0.00283	0.0002040
89.0	0.00	0.07	0.073	0.00263	0.0001899
90.0	0.00	0.07	0.068	0.00245	0.0001766
91.0	0.00	0.06	0.064	0.00228	0.0001643
92.0	0.00	0.06	0.059	0.00212	0.0001529
93.0	0.00	0.06	0.055	0.00197	0.0001423
94.0	0.00	0.05	0.051	0.00184	0.0001324
95.0	0.00	0.05	0.048	0.00171	0.0001232
96.0	0.00	0.04	0.044	0.00159	0.0001146
97.0	0.00	0.04		0.00148	0.0001067
98.0	0.00	0.04	0.039	0.00139	0.00000035
99.0	0.00	0.04	0.039	0.00138	0.00000035
100.0	0.00	0.04	0.038	0.00138	0.00000035



## Nomenclature

A	Area
a	Speed of sound
C	Constant
$c_p$	Pressure coefficient
M	Mach number
m	Mass
$\dot{m}$	Mass flow rate
n	Correction factor exponent
p	Pressure
$p_c$	Cracking pressure differential
Q	Volume flow rate
R	Gas constant
T	Temperature
t	Time
V	Volume
v	Velocity
$\gamma$	Ratio of specific heats
$\rho$	Density

## Subscripts

atm	Atmospheric conditions
crit	Critical (at $M = 1$ )
e	Exit, external
f	Filters
i	Inlet, internal
l	Leaks
o	Orifices
T	Total
v	Valves
1	Primary volume internal
2	Secondary volume internal